Ramanujan 1914, approximation to Pi

$$\begin{split} OB &= 1, AT = 1/3, MC = 1/3 = MN, AM = AP, PQ||NM, TR||OQ, AS = AR\\ OW &= 1/2OS, \angle OVU = 90^\circ, \ OU \ \text{approximates} \ \pi/3 \ \text{with} \ 9 \ \text{digits}\\ OU &= \frac{1}{3} \left(9^2 + \frac{19^2}{22}\right)^{1/4} = \frac{1}{3} \left(2143/22\right)^{1/4} \approx 1.04719755086089. \ \pi/3 \approx 1.04719755119660. \end{split}$$



Found in S. Ramaujan, "Modular Equations and Approximations to π ", Collected Papers (G. H. Hardy, P. V. Seshuaigar and B. M. Wilson, Eds.), Chelsea, New ork, 1922, pp. 23-39.

Reprinted in "Pi: A Source Book" (L. Berggren, J. Borwein and P. Borwein, Eds.) Springer, New York, 1997, pp. 241-257. Construction on pp.253-4.

OU, the square root of OS, has been constructed from the geometric mean of OV=1 and OS (not shown in Ramanujan's original figure 2.)

T is obtained as projection of a point Y along the CO direction. Y is the intersection point of the lines AC and 0X where X is the midpoint of the parallel to CO through A.

Put on the web by Wolfdieter Lang, June 2007.