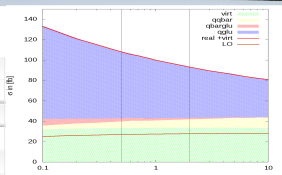


# NLO-QCD Corrections to (WZ)/W $\gamma$ -Production at LHC

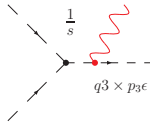
Karlsruhe Institute of Technology (KIT)  
Johannes Bellm | December 15, 2011

INSTITUTE FOR THEORETICAL PHYSICS



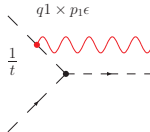
- 1 Motivation
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- missing process in VBFNLO
- large K-factor (3.5) (radiation zero, gluon-pdf)
- sensitive to anomalous couplings
- comparison to MCFM



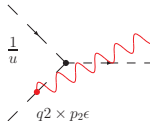
$$\text{Amplitude: } M = \sum_i \frac{q_i \times p_i \epsilon}{p_i p_\gamma} = \sum_i \frac{A_i \times B_i}{C_i}$$

- A: charge conservation:  $\sum_i q_i = 0$
- B: transverse polarization:  $\sum_i p_i \epsilon = p_\gamma \epsilon = 0$
- C:  $m_\gamma = 0$ :  $\sum_i p_i p_\gamma = p_\gamma p_\gamma = 0$



$$\rightarrow M = \sum_i \frac{A_i \times B_i}{C_i} = \frac{1}{C_3} (A_1 C_2 - A_2 C_1) \left( \frac{B_2}{C_2} - \frac{B_1}{C_1} \right)$$

So the amplitude gets zero when:



$$\frac{Q_1}{Q_2} = \frac{t}{u}$$

# Radiation Zero

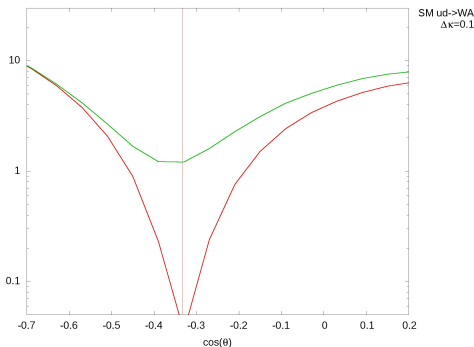
In the standard model there is a triple vertex  $q\bar{q}W$ . From every leg a photon can be radiated.

- A: generalized Jacobi identity (group-theory)
- B: spatial gen. Jacobi identity (see gen. Bianchi identity in GR)
- C:  $s - M_W^2 + t + u = 0$

we get:

$$\frac{d\sigma(d\bar{u} \rightarrow W^- \gamma)}{d\cos\theta_{W-d}} = \left( \frac{q_{\bar{u}}}{q_d} - \frac{t}{u} \right)^2$$

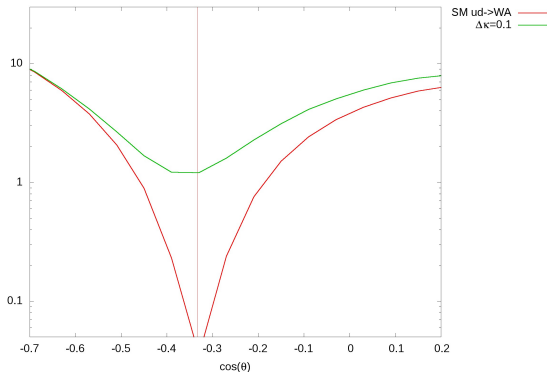
the amplitude vanishes  
for  $\cos\theta = -1/3$



# Radiation Zero

with anomalous vertex for  $WW\gamma$ ,  
(no local gauge theory, no covariant derivative):

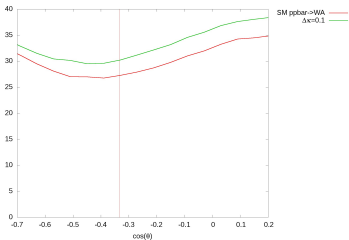
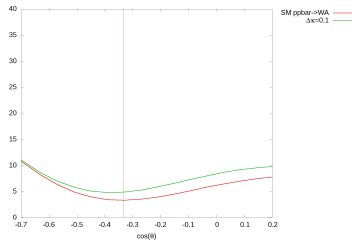
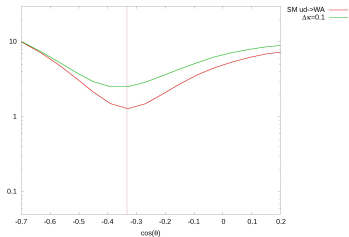
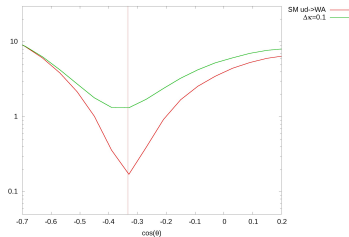
$$\frac{\sigma(d\bar{u} \rightarrow W^{-}\gamma)}{d\cos\theta_{W^{-}d}} = \left(\frac{q_{\bar{u}}}{q_d} - \frac{t}{u}\right)^2 \Gamma_1 + (\kappa - 1) \left(\frac{q_{\bar{u}}}{q_d} - \frac{t}{u}\right) \Gamma_2 + (\kappa - 1)^2 \Gamma_3$$



zero-conditions:

- final W on shell
- no final state radiation
- $q\bar{q}$  collider
- only QCD-LO

# Radiation Zero



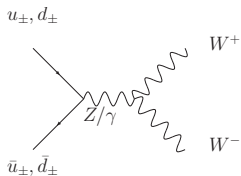
K-factors for diboson production and the effect of radiation zero:

$W^+ W^-$	1.5
$W^\pm Z$	1.9
$W^\pm \gamma$	3.5

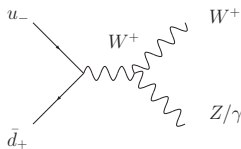


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Differences to  $W^+ W^-$  (V.Hankele):



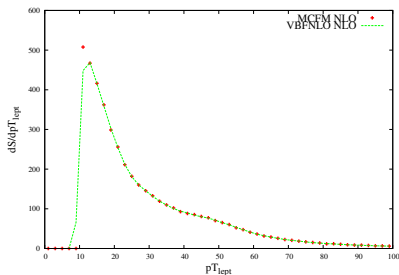
+++++



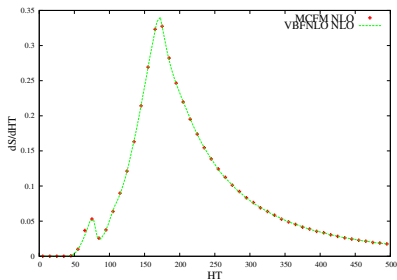
- $WZ/W\gamma$  has always left(right)handed incoming (anti)fermions [W attachment]
- outgoing fermions from  $Z/\gamma^*$  or  $\gamma$  itself can have  $\pm$ -helicities
- new combination of PDFs (as in  $WZZ$  or  $W\gamma\gamma$ )
- additional anomalous couplings have been added (B.Feigl)
- new phase space generator needed
- the NLO-QCD part is basically the same!

- In the code:  $|M|^2$  comparison with automatic generated MADGRAPH-code ( $\mathcal{O}(10^{-7})$ )
- LO: comparison with SHERPA ( $\mathcal{O}(10^{-3})$ )
- NLO: comparison with MCFM ( $\mathcal{O}(10^{-3})$ )

$W^+\gamma$



$W^-Z$



- VBFNLO has  $W^\pm \gamma j$  and  $W^\pm Zj$  @ NLO with anomalous couplings (Englert)
- different implementations of the triboson vertices (Feigl,Englert)
- differences appear  $\rightarrow$  could be solved:

$(f_{www}; f_w; f_b), \text{FORM}$	$W^+ Z \text{ LO } +j$ (310)	$W^+ ZJ \text{ LO}$ (640)	ratio
$(0;0;0), \text{ off (SM)}$	36.109	36.122	0.99966
$(1; 0; 0) \cdot 10^{-4}, \text{ off}$	348.377	348.408	0.99991
$(0; 6; 0) \cdot 10^{-4}, \text{ off}$	4272.325	4271.854	1.00011
$(0; 0; 1) \cdot 10^{-3}, \text{ off}$	66.825	66.821	1.00006
$(0.5; 2; 6) \cdot 10^{-4}, \text{ off}$	573.984	573.568	1.00073
$(0.5; 2; 6) \cdot 10^{-4}, \text{ on}$	342.127	342.300	0.99950

# Catani-Seymour Subtraction Formalism

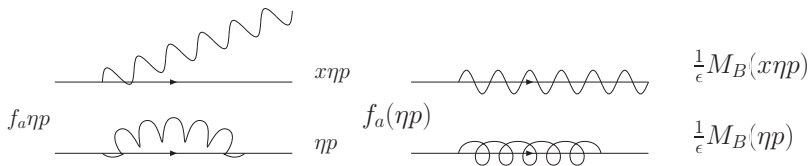
- dipole formalism (Martin's talk)
- no jets @ LO
- LHC  $\rightarrow$  two initial state hadrons
- new collinear term  $\rightarrow$  PDF-renormalization (Karol's talk)

# Catani-Seymour Subtraction Formalism

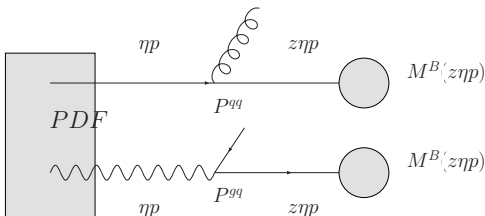
DIS:

$$\sigma^{NLO}(p) = \sum_a \int_0^1 d\eta \underbrace{f_a(\eta)}_{PDF} \left[ \int_m d\sigma_a^V(\eta p) + \int_{m+1} d\sigma_a^R(\eta p) + \underbrace{\int_m d\sigma_a^C(\eta p)}_{coll. CT} \right]$$

- Why do we need the collinear counterterm?



$$d\sigma_a^C(\eta p) = -\frac{\alpha_s}{2\pi} \frac{1}{\Gamma(1-\epsilon)} \sum_b \int_0^1 dx \left[ -\frac{1}{\epsilon} \left( \frac{4\pi\mu^2}{\mu_F^2} \right)^\epsilon P^{ab}(x) + \dots \right] d\sigma_b^B(x\eta p)$$



next step:

- construct local counter term with dipoles  $D^{ai,b}$  (Martins talk)
- integrate out the additional jet in d-Dimensions

We get:

$$\int_{m+1} d\sigma_a^A(p) + \int_m d\sigma_a^C(p) =$$
$$\int_m \underbrace{[d\sigma_a^B(p) I(\epsilon)]}_{\text{cancels } d\sigma^V} + \underbrace{\sum_b \int_0^1 dx (\mathbf{K}^{a,b}(x) + \mathbf{P}^{a,b}(xp)) d\sigma_b(xp)}_{\text{remormalisation of PDF}}$$



Different approach:

$$\begin{aligned} \sigma(p) &= \sum_a \int_0^1 d\eta f_a(\eta) \sigma_a(\eta p) = \\ &= \sum_{a,b} \int_0^1 d\eta dz f_a(\eta) (\delta_{ab} \delta(1-z) + \alpha_s \tilde{P}_{ab}(z)) (\sigma_b^{LO}(\eta zp) + \sigma_b^{NLO}(\eta zp)) + \dots \end{aligned}$$

$$\begin{aligned} \sigma^{NLO}(p) &= \sum_a \int_0^1 d\eta f_a(\eta) \sigma_a^{NLO}(\eta p) \\ &+ \sum_{a,b} \int_0^1 d\eta' JF dz' \alpha_s f_a(z', \eta') \tilde{P}_{ab}(z', \eta') \sigma_b^{LO}(\eta' p) \end{aligned}$$

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$WW_\gamma$  terms in an effective Lagrangian (CP-conserving):

$$\mathcal{L}_{WW_\gamma} = -ie \left[ W_{\mu\nu}^\dagger W^\mu A^\nu - W_\mu^\dagger A_\nu W^{\mu\nu} + \kappa_\gamma W_\mu^\dagger W_\nu F^{\mu\nu} + \frac{\lambda_\gamma}{m_W^2} W_{\sigma\mu}^\dagger W_\nu^\mu F^{\nu\sigma} \right]$$

- $\kappa_\gamma=1, \lambda_\gamma = 0 \rightarrow$  SM
- Sep11(Fermilab):  $0.6 < \kappa_\gamma < 1.4$  ,  $-0.08 < \lambda_\gamma < 0.07$
- unitary problems for high energy behavior:  $\hat{s} + u + t$ -channel (see  $WW$ -scattering without a higgs)
- formfactor needed:

$$\frac{1}{\left(1 + \frac{s}{\Lambda^2}\right)^n}$$

For the high energy ( $m_W/\sqrt{s} \rightarrow 0$ ) behavior we take a look at the  $\Delta M_{\sigma_\gamma \sigma_W}(\Delta\kappa, \lambda)$ :

$$\Delta M_{\pm 0} = \frac{e^2}{\sin(\theta_W)} \frac{\sqrt{s}}{2m_W} [\Delta\kappa + \lambda] \frac{1}{2} (1 \mp \cos\Theta) \quad (1)$$

$$\Delta M_{\pm\pm} = \frac{e^2}{\sin(\theta_W)} \frac{s}{2m_W^2} [\lambda] \frac{1}{\sqrt{2}} (\sin\Theta) \quad (2)$$

$$\Delta M_{\pm\mp} = 0 \quad (3)$$

The third amplitude is not possible because of s-channel exchange.  $(\pm, \mp)$  needs  $J \geq 2$

- Wj-production with misidentified jet is serious  $\rightarrow p_{T\gamma} > 100\text{GeV}$
- $M_T(l\gamma, \nu)^1 > 90\text{GeV}$ ,  $R(l, \gamma)^2 > 0.7$  together with high  $p_{T\gamma}$  suppresses final state bremsstrahlung
- For  $O = p_{T\gamma}$  a  $p_{Tj}$ -veto =  $50\text{GeV}$

---

$$^1 M_T(l\gamma, \nu) = [(m(l\gamma)^2 + |p_T(l\gamma)|^2)^{1/2} + |\not{p}_T|^2 - |p_T(l\gamma) + \not{p}_T|^2]$$

$$^2 R = \sqrt{\Delta\eta^2 + \Delta\phi^2}$$

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$$\sigma^{N^n LO} \rightarrow \sigma^{N^{n+1} LO}$$

With this step one get an new real emission, a new jet.

What is an inclusive X-section?

Define:

$$\sigma_{incl}(W\gamma) = \sigma_{excl}(W\gamma) + \sigma_{excl}(W\gamma j) + \sigma_{excl}(W\gamma jj) + .. \quad (4)$$

$$= \sum_n \sigma_{excl}(W\gamma(n \times j)) \quad (5)$$

How to define a exclusive X-section?

$$\sigma_{incl}(W\gamma) = \sigma_{excl}(W\gamma) + \sum_n \sigma_{excl}(W\gamma j(n \times j)) \quad (6)$$

$$= \sigma_{excl}(W\gamma) + \sigma_{incl}(W\gamma j) \quad (7)$$

so:

$$\sigma_{excl}(W\gamma) = \sigma_{incl}(W\gamma) - \sigma_{incl}(W\gamma j) \quad (8)$$



$\mathcal{O}(\alpha_s)$ :

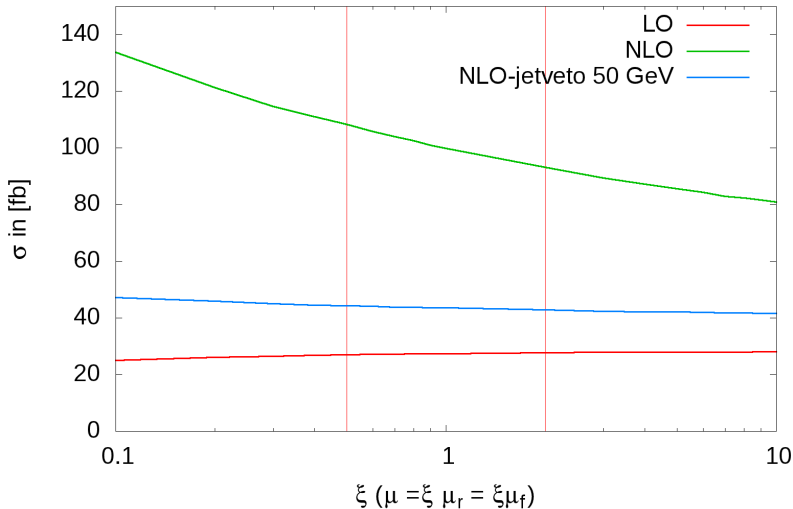
$$\sigma_{excl}^{NLO}(W\gamma) = \sigma_{incl}^{NLO}(W\gamma) - \sigma_{incl}^{LO}(W\gamma j) = \sigma_{veto}^{NLO}(W\gamma) \quad (9)$$

Next question: Whats the theoretical uncertainty for  $\sigma_{veto}^{NLO}$ ?

- scale variation of the difference?
- say  $\sigma_{incl}^{NLO}(W\gamma)$  and  $\sigma_{incl}^{LO}(W\gamma j)$  are independent? Scale estimated uncertainties have to sum up?
- a new way?

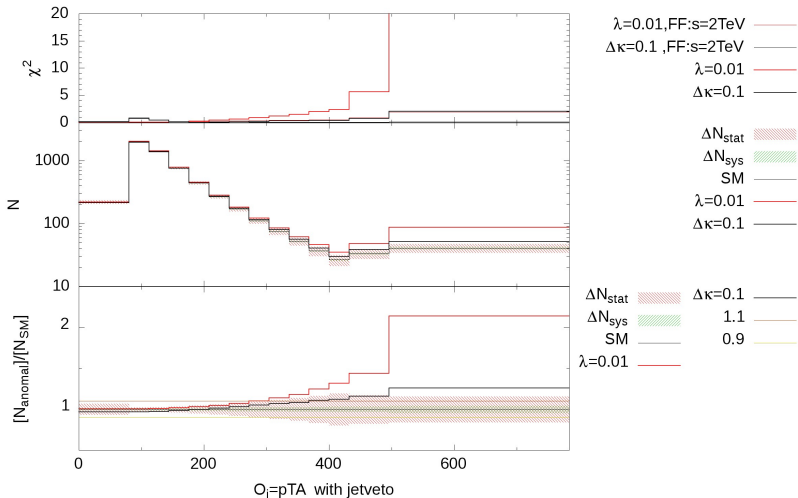
# Inclusive vs. Exclusive

Scaledependence



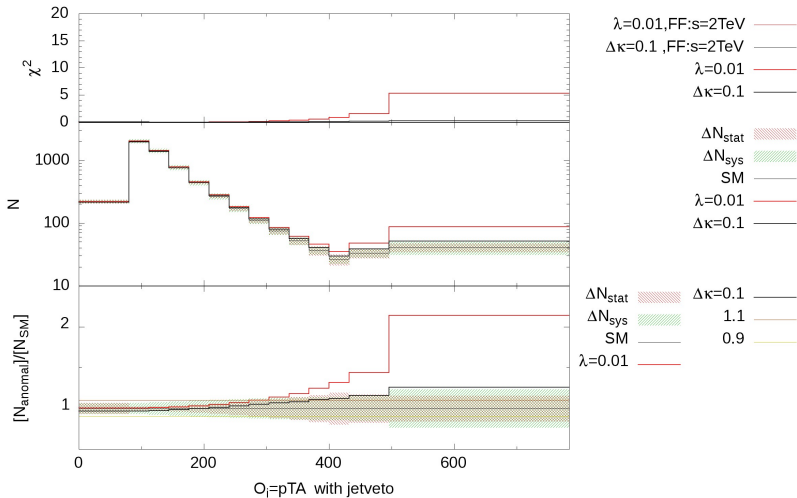
# Scale Variation of the Difference

Informations:  $100 \text{ fb}^{-1}$ ,  $N > 20 \text{ events/bin}$ ,  $s=14 \text{ TeV}$ ,  $\chi^2=(N_{\text{ano}}-N_{\text{SM}})^2/(N_{\text{SM}}+\Delta N_{\text{sys}}^2)$



# Independent Scale Variation

Informations:  $100 \text{ fb}^{-1}$ ,  $N > 20 \text{ events/bin}$ ,  $s=14 \text{ TeV}$ ,  $\chi^2 = (N_{\text{ano}} - N_{\text{SM}})^2 / (N_{\text{SM}} + \Delta N_{\text{sys}})^2$



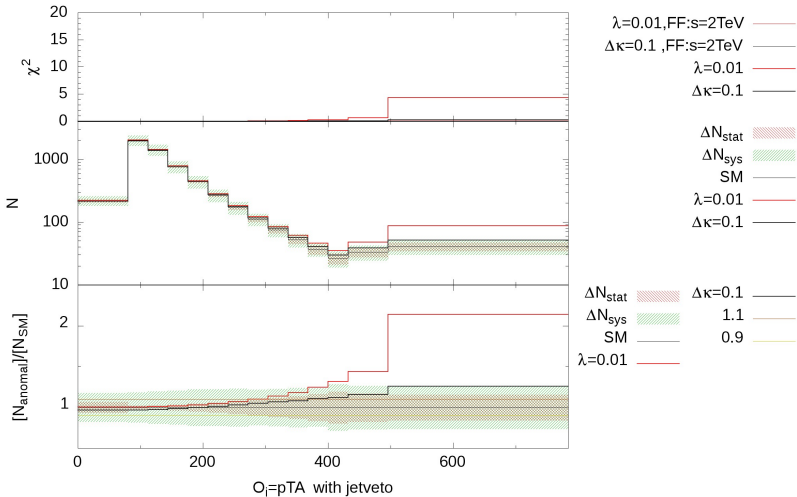
$$\Delta\sigma_{excl}^{NLO}(W\gamma) = \Delta\sigma_{incl}^{NLO}(W\gamma) + \Delta\sigma_{incl}^{LO}(W\gamma j)$$

*with :*

$$\Delta\sigma_{incl}^{NLO}(W\gamma) = \frac{1}{2}(|\sigma_{incl}^{NLO}(W\gamma)_{\xi=2} - \sigma_{incl}^{NLO}(W\gamma)_{\xi=0.5}|)$$

$$\Delta\sigma_{incl}^{LO}(W\gamma j) = |\sigma_{incl}^{NLO}(W\gamma j) - \sigma_{incl}^{LO}(W\gamma j)|$$

Informations:  $100 \text{ fb}^{-1}$ ,  $N > 20 \text{ events/bin}$ ,  $s=14 \text{ TeV}$ ,  $\chi^2 = (N_{\text{ano}} - N_{\text{SM}})^2 / (N_{\text{SM}} + \Delta N_{\text{sys}})^2$



# New Way and Independent Scale Variation

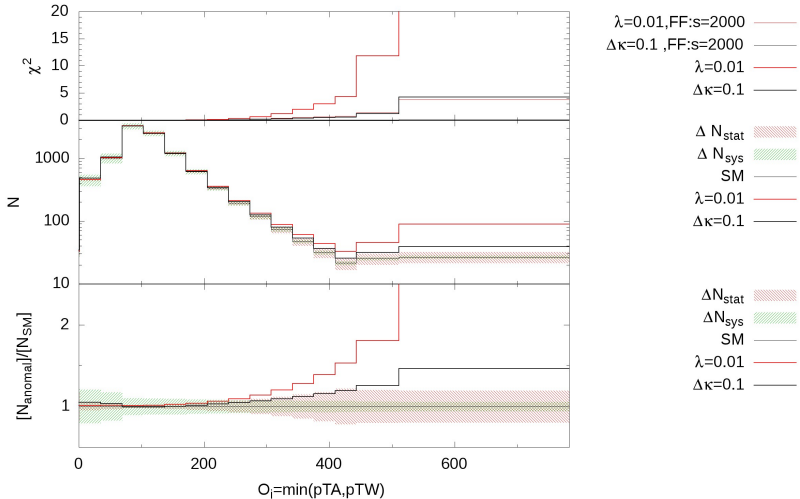
Pro:

- The vetoed  $\sigma$  is less inclusive  $\rightarrow$  large logarithms can appear.  
@ every order of perturbation theory.
- Fine tuning of the uncertainty cannot be done.
- For  $W_{\gamma j}$  @ LO we have the best estimation for the error with the NLO-calculation.

Contra:

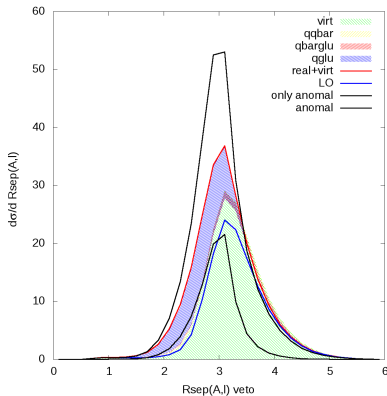
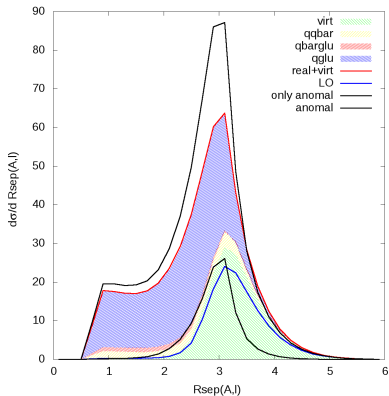
- In  $\mathcal{O}(\alpha_s^2)$  more jets appear  $\rightarrow$  a cut on  $E_{had}$  suppresses higher order contributions
- Overestimation? doublecounting of the uncertainty coming from  $W_{\gamma j}$  @ LO

Informations:  $100 \text{ fb}^{-1}$ ,  $N > 20 \text{ events/bin}$ ,  $s=14 \text{ TeV}$ ,  $\chi^2=(N_{\text{ano}}-N_{\text{SM}})^2/(N_{\text{SM}}+\Delta N_{\text{sys}}^2)$





# New Cuts

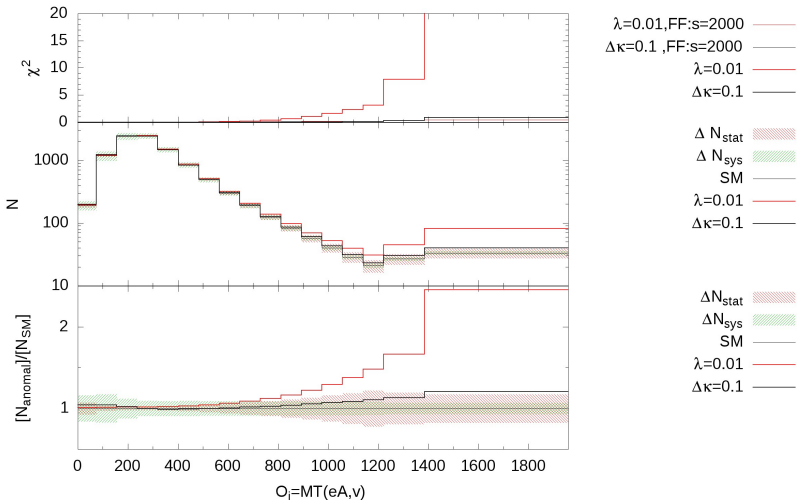


Is this infrared safe?

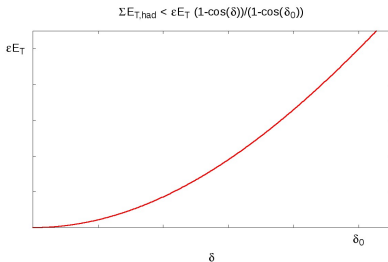
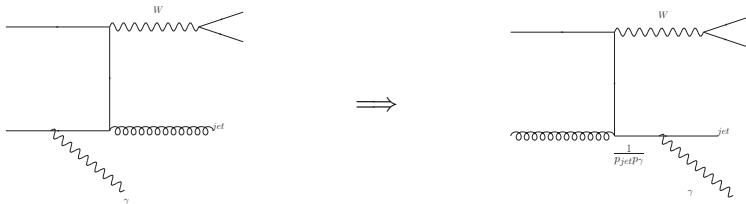
- what influence has  $gg \rightarrow W\gamma jj$ ? ( $W\gamma j$ @NLO)
- New cuts for inclusive searches.
- $Wj$  Process not yet available, but 'easy' to get from  $WVj$  or  $WVj$  (different structure)
- make the analysis for  $WZ$  production

Thank you for your attention!

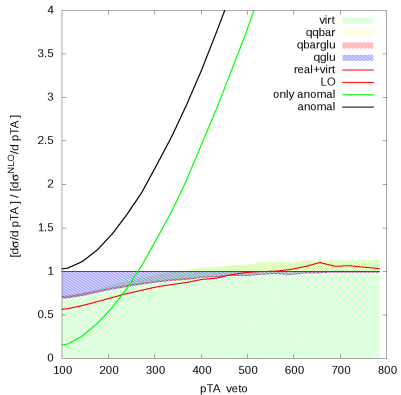
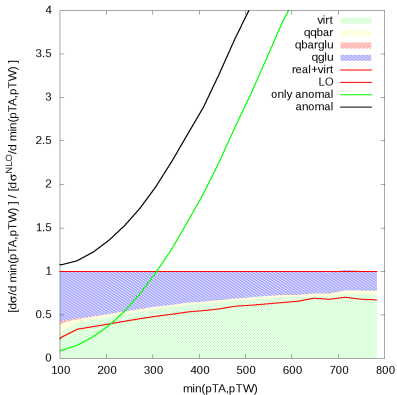
Informations:  $100 \text{ fb}^{-1}$ ,  $N > 20 \text{ events/bin}$ ,  $s=14 \text{ TeV}$ ,  $\chi^2=(N_{\text{ano}}-N_{\text{SM}})^2/(N_{\text{SM}}+\Delta N_{\text{sys}}^2)$



# Photon isolation à la Frixione



# $pT_\gamma$ vs. $\min(pT_\gamma, pT_W)$



# Inclusive vs. Exclusive

