Determination of Higgs Couplings at the LHC

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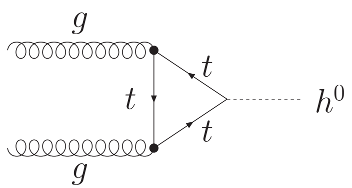
Outline

- Production and Decay of Higgs Bosons
- Analysis of Effective Higgs Couplings
- Supersymmetric Scenario
- Combining Poisson and Gaussian Errors
- Determination of Errors on Couplings

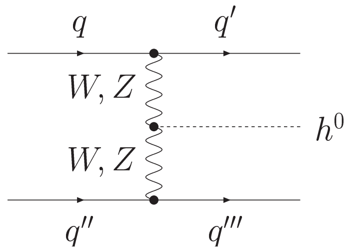
Production Modes

Main Higgs-boson production modes:

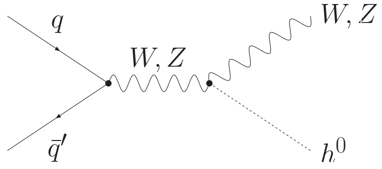
- Gluon-Gluon Fusion



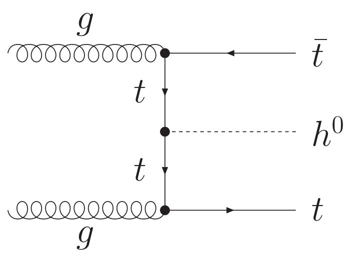
- Vector-Boson Fusion

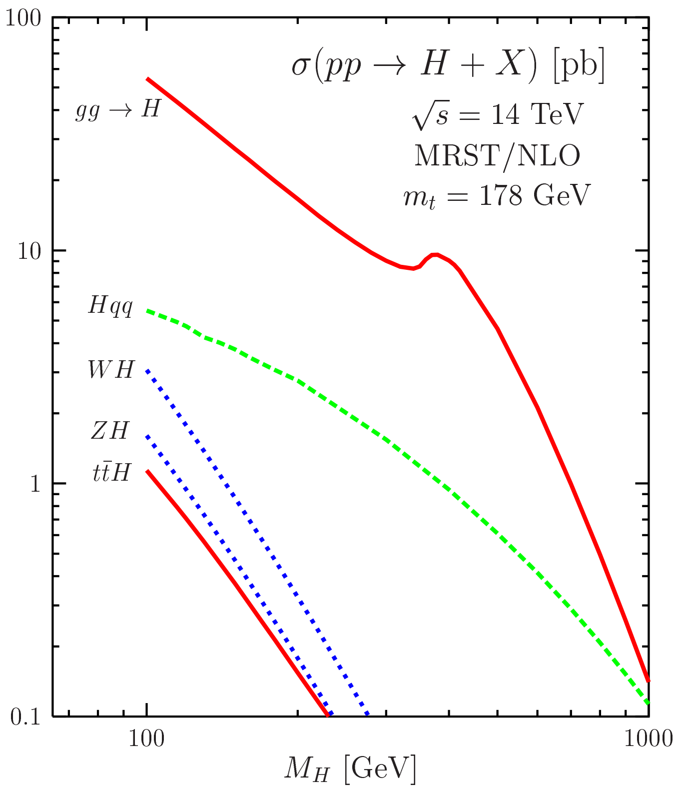


- Associated Production with a Gauge Boson



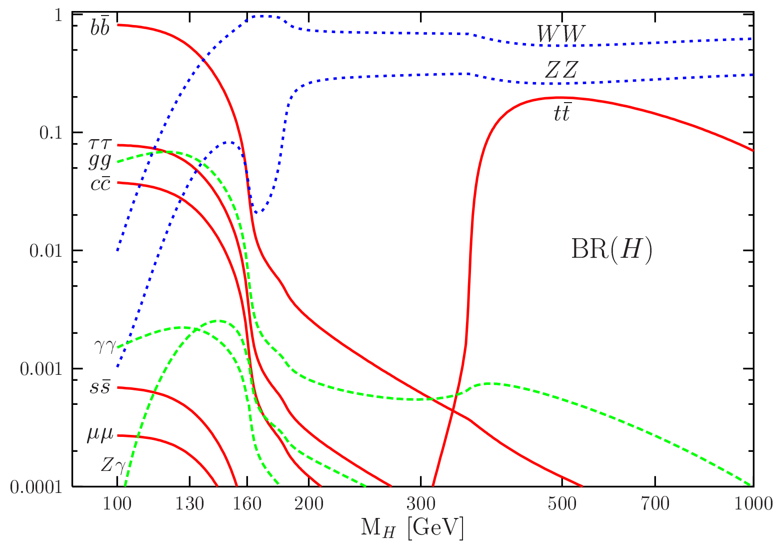
- Associated Production with Top-Quark–Antiquark Pair





Higgs-Boson Decays

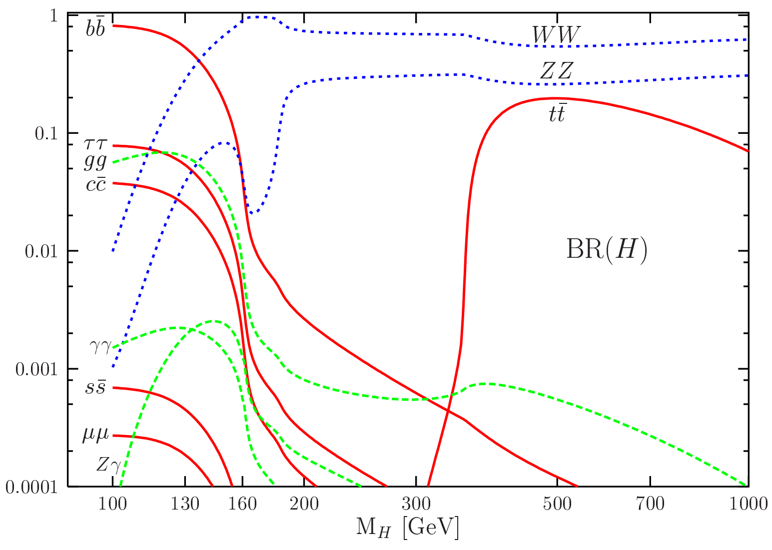
- $H \to b\bar{b}$
  - Main decay mode ($\sim 90\%$) for light Higgs bosons, as suggested by electroweak precision data
  - Hard to extract from QCD backgrounds
  - Combination with ttH production difficult to observe because of combinatorial background (4 bottom quarks in final state)
  - Recent suggestion of WH/ZH production plus jet substructure analysis looks promising



[CMS-TDR]

Higgs-Boson Decays

- $H \to b\bar{b}$
- $H \to WW$
  - Main decay mode for heavier Higgs bosons ($m_H \gtrsim 140$ GeV)
  - Two leptonic decays of the W allow only reconstruction of transverse mass of the WW pair
  - Gluon and vector-boson fusion relevant even if Ws are off-shell

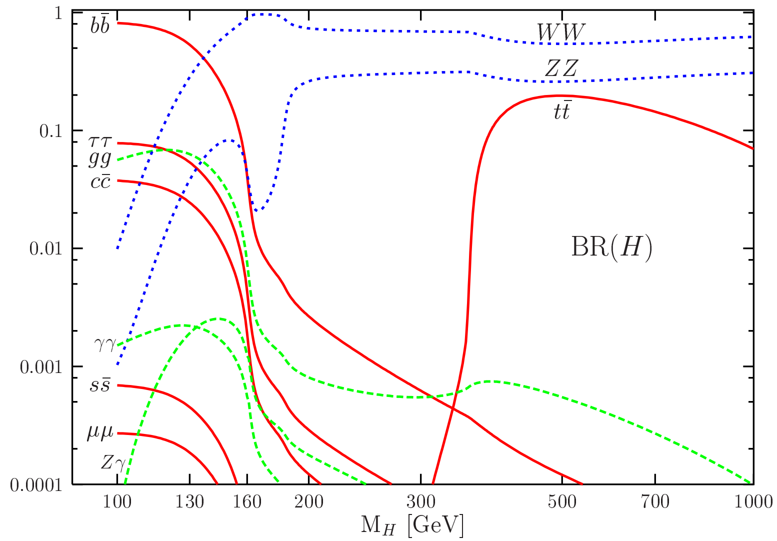


[CMS-TDR]

Higgs-Boson Decays

- $H \to b\bar{b}$
- $H \to WW$
- $H \to ZZ$
  - “Golden Channel” due to four-lepton final state
  - Statistically limited to larger Higgs masses
- $H \to \tau\tau$
  - Need to reconstruct invariant mass of the two taus
  - Limits production channel to vector-boson fusion
  - One of the discovery channels for light Higgs bosons

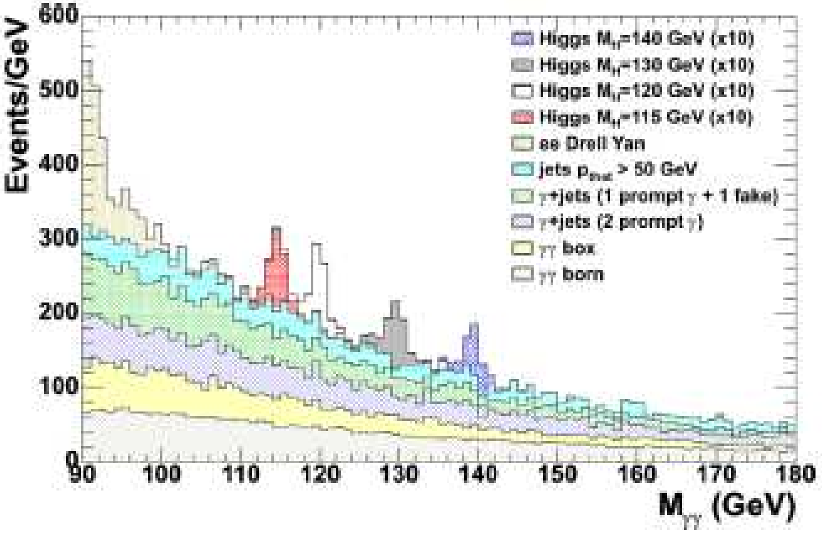
[Plehn, Rainwater, Zeppenfeld]



[CMS-TDR]

Higgs-Boson Decays

- $H \to b\bar{b}$
- $H \to WW$
- $H \to ZZ$
- $H \to \tau\tau$
- $H \to \gamma\gamma$
  - Loop-induced coupling by (mainly) W and t
  - Only fully reconstructable channel for a light Higgs boson
  - Small branching ratio ($\lesssim 0.2\%$)
  - Promising discovery channel for light Higgs bosons, background can be subtracted via sidebands
  - Higgs mass measurement up to 100 MeV



[CMS-TDR]

General Higgs Sector

- Theory: Standard Model plus general Higgs sector
- For Higgs couplings present in the Standard Model $j = W, Z, t, b, \tau$ replace general couplings by

$$g_{jjH} \longrightarrow g_{jjH}^{\text{SM}} \left(1 + \Delta_{jjH}\right)$$

- For loop-induced Higgs couplings $j = \gamma, g$ replace by

$$g_{jjH} \longrightarrow g_{jjH}^{\text{SM}} \left(1 + \Delta_{jjH}^{\text{tree}} + \Delta_{jjH}\right)$$

where g_{jjH}^{SM}: (loop-induced) coupling in the Standard Model
$\Delta_{jjH}^{\text{tree}}$: contribution from modified tree-level couplings to Standard-Model particles
Δ_{jjH}: additional (dimension-five) contribution

- Additional free parameters:
  - Higgs boson mass m_H
  - Top-quark mass m_t
  - Bottom-quark mass m_b
- Experimental input:
  - ATLAS study on Higgs couplings [Dührssen, references therein; ATLAS & CMS-TDR]
  - Jet substructure analysis for WH/ZH, $H \rightarrow b\bar{b}$ [Butterworth, Davison, Rubin, Salam]

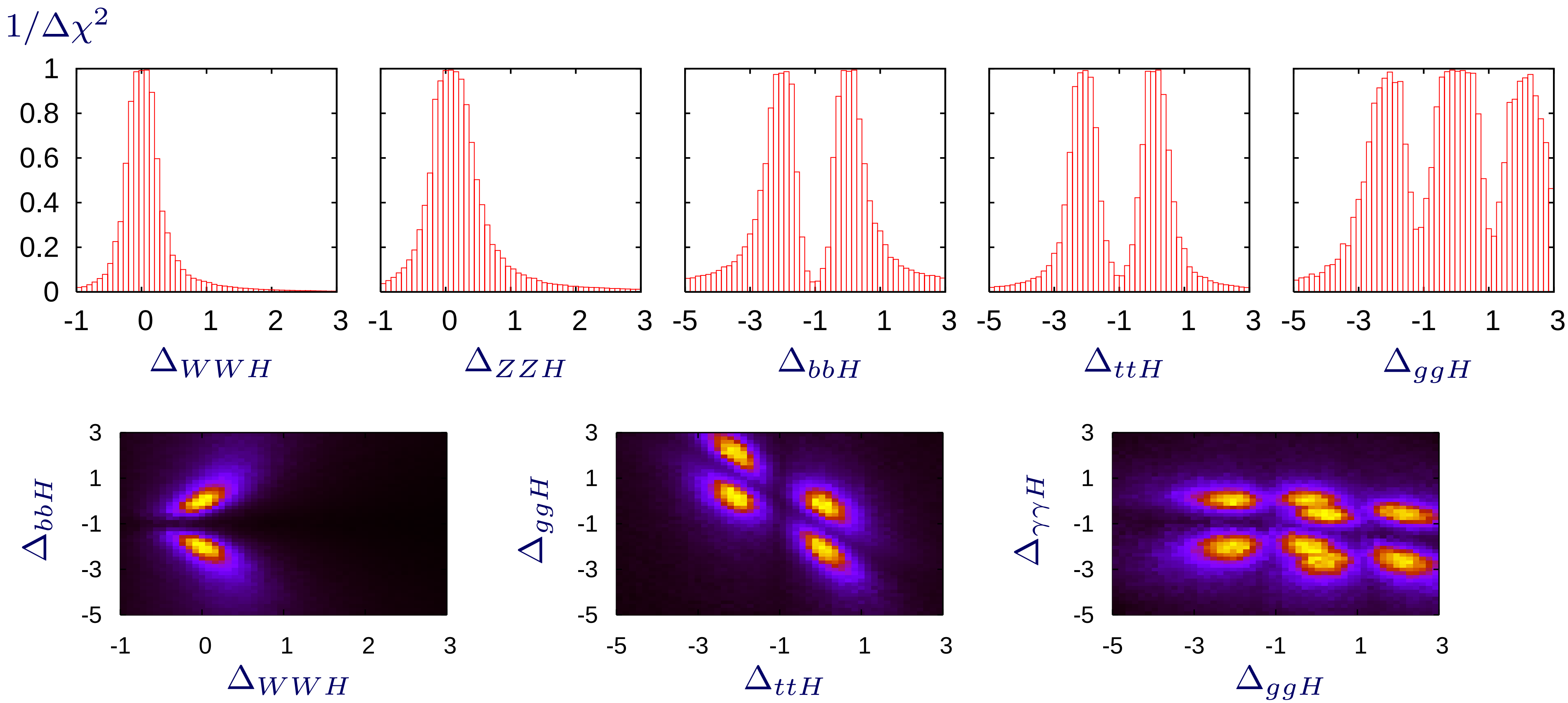
SFitter

- Need to scan high-dimensional parameter space
- $\Rightarrow$ SFitter [Lafaye, Plehn, MR, Zerwas]
- General Higgs couplings from modified version of HDecay [Spira]
- Three scanning techniques:
  - Weighted Markov Chain
  - Cooling Markov Chain (equivalent to simulated annealing)
  - Gradient Minimisation (Minuit)
- Output of SFitter:
  - Fully-dimensional log-likelihood map
  - Reduction to plotable one- or two-dimensional distributions via both
    - Bayesian (marginalisation) or
    - Frequentist (profile likelihood) techniques
  - List of best points

Results

LHC data set with $30\ \text{fb}^{-1}$, $m_H = 120$ GeV , Profile likelihood

True data set

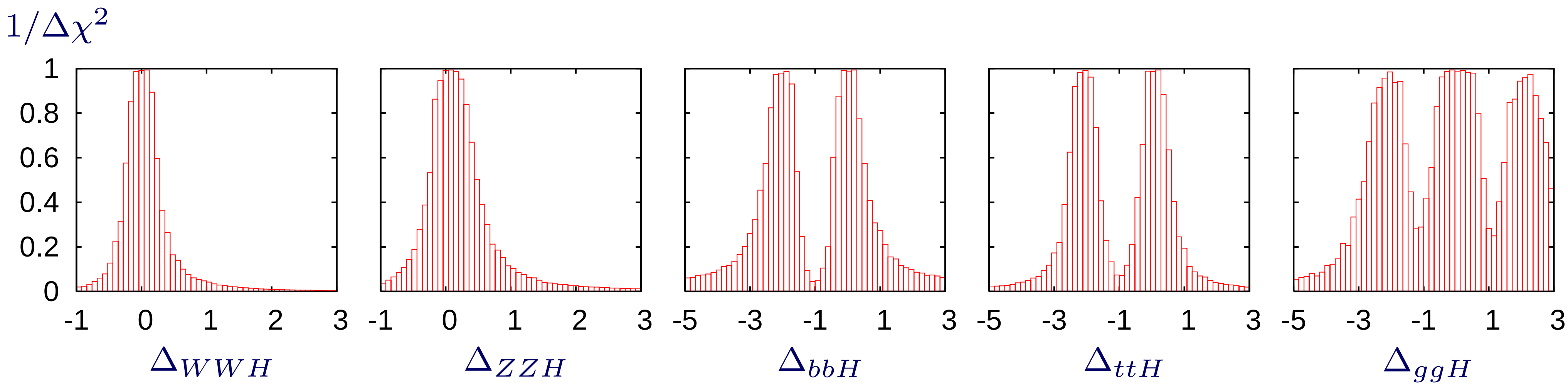


- Can reconstruct Standard Model solution, alternative solutions due to sign degeneracy
- See expected correlations (e.g. Δ_{ttH} vs Δ_{ggH})

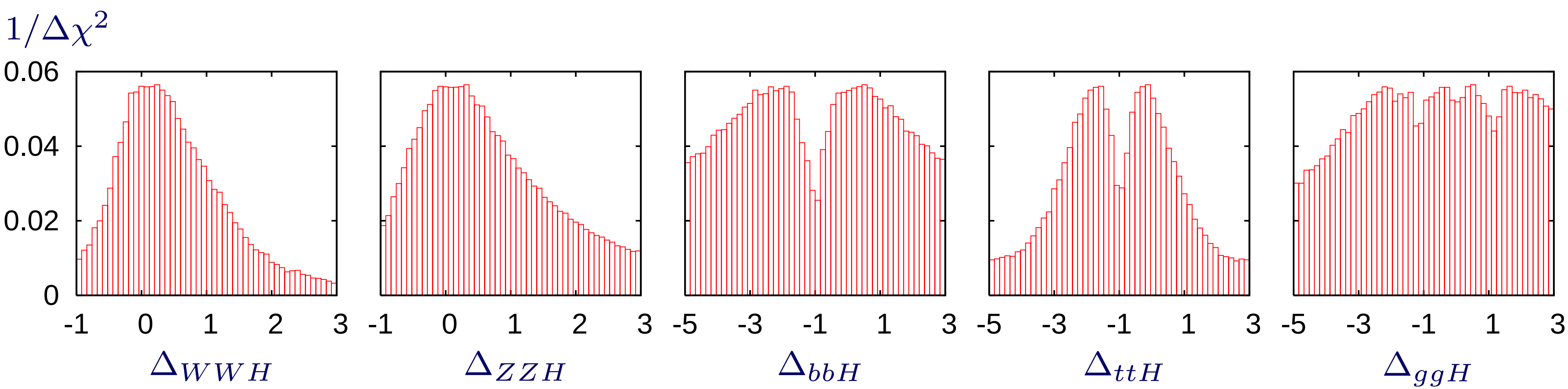
Results

LHC data set with $30\ \text{fb}^{-1}$, $m_H = 120$ GeV , Profile likelihood

True data set

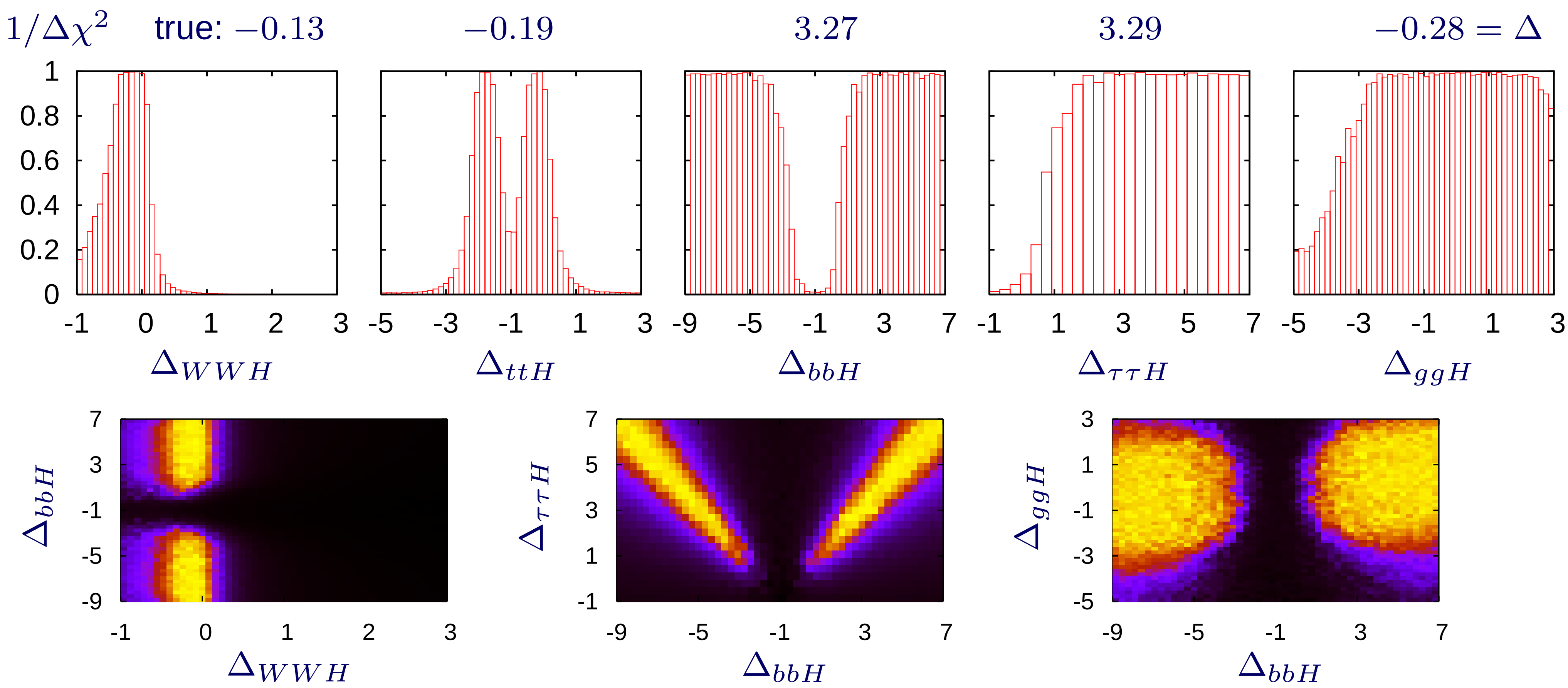


Smeared data set



Non-decoupling Supersymmetric Higgs

SPS1a-inspired scenario with $t_\beta = 7$, $A_t = -1100$ GeV , $m_A = 151$ GeV , $m_{h^0} = 120$ GeV
LHC data set with 30 fb^{-1}, Profile likelihood, true data set



- Clear deviation from Standard Model: $\Delta\chi^2 = 444/18$ dof $\quad\hat{=}\quad$ CL $= 1 - 10^{-83}$
- Strong correlation between Δ_{bbH} and $\Delta_{\tau\tau H}$ via total width
- No upper limit on g_{bbH} as $BR \simeq 1$ compatible with data

Errors

- Statistical errors on individual channels of Poisson type
- Systematic errors (luminosity, tagging efficiency, . . .) extracted from large event samples $\Rightarrow$ Gaussian
- Need to combine
  - Poisson $P_P(d,m) = \frac{\exp(-m)m^d}{\Gamma(d+1)}$ and
  - Gaussian $P_G(d,m,\sigma) = \frac{1}{\sqrt{2\pi}\sigma}\exp(-\frac{(d-m)^2}{2\sigma^2})$ errors
- Mathematically correct way: convolution
- No analytic solution, numerical integration too time-consuming
- $\Rightarrow$ Approximate formula:

$$\frac{1}{\tilde{\chi}^2} \equiv \frac{1}{-2\log L} = \sum_i \frac{1}{-2\log L_i}$$

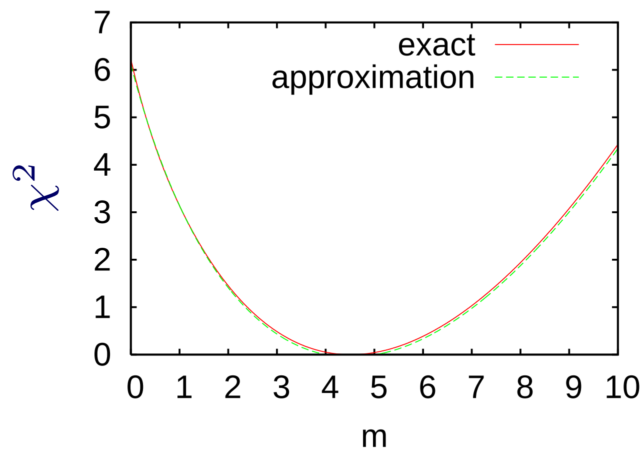
  - Yields exact formula for Gaussian-only (adding errors in quadrature)
  - Gives correct result when one error approaches 0 or ∞

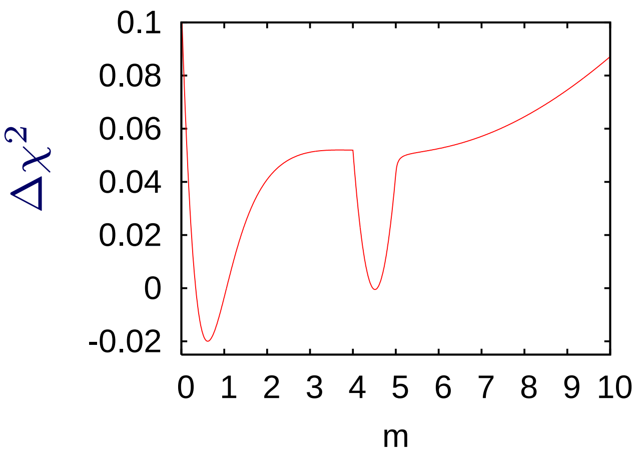
Errors

- Approximate formula for Gauss and Poisson errors:

$$\frac{1}{\tilde{\chi}^2} = \frac{1}{-2\log L} = \sum_i \frac{1}{-2\log L_i}$$
$$\rightarrow \frac{1}{-2\log L_P} + \frac{1}{-2\log L_G}$$
$$= \frac{1}{-2\log P_P(d,m)/P_P(m,m)} + \frac{\sigma^2}{-2(d-m)^2}$$

- Example: Poisson($d = 5$), Gauss($\sigma = 0.5$)





- $\Rightarrow$ Very good agreement with exact convolution
- Difference almost always positive $\Rightarrow$ slight overestimation of Higgs-coupling errors (good!)

Determination of errors on couplings

Determination of errors on Higgs couplings:

- Perform 10,000 toy experiments with measurements smeared around correct value
- Minimise each toy experiment
- Plot resulting distribution of parameter points and fit with Gaussian

	full measurements			only $t\bar{t}H$, $H \to b\bar{b}$		
	σ_{symm}	σ_{neg}	σ_{pos}	σ_{symm}	σ_{neg}	σ_{pos}
m_H	± 0.25	-0.26	$+0.25$	± 0.25	-0.26	$+0.25$
$\Delta_{b\bar{b}H}$	± 0.44	-0.30	$+0.59$	± 0.78	-0.43	$+0.84$
Δ_{WWH}	± 0.24	-0.21	$+0.27$	± 0.33	-0.24	$+0.43$
$\Delta_{\tau\bar{\tau}H}$	± 0.31	-0.19	$+0.46$	± 0.39	-0.20	$+0.60$
Δ_{ggH}	± 0.61	-0.59	$+0.62$	± 0.66	-0.48	$+0.82$

- Can determine all couplings with good accuracy
- Subjet analysis crucial for precise determination of $g_{b\bar{b}H}$
  Without this additional peak at $g_{b\bar{b}H} = 0$ (not fitted abvove)
- Accuracy on $g_{b\bar{b}H}$ feeds back into all other couplings via total width

Summary

- Determining the Higgs-boson couplings next step after discovery
  Important for our understanding of electroweak symmetry breaking
- Independent of explicit realisation of new physics (if any):
  Standard Model with effective Higgs couplings
- Problem of high-dimensional parameter space with correlated measurements
  $\Rightarrow$ Dedicated tool: SFitter

- Obtain Standard Model couplings within errors for SM scenario
- Alternative solutions due to sign degeneracy of couplings
- Clear deviation for non-degenerate SPS1a-inspired scenario

- Analysis of errors on couplings
- Recent jet substructure analysis significantly improves result on bottom-quark coupling
- Influences accuracy of all other couplings via total width