

# Vector-Boson-Scattering – VBFNLO update

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INSTITUTE FOR THEORETICAL PHYSICS



- VBFNLO overview
- Recent enhancements
  - Semileptonic decays
  - Form factor tool
- Backgrounds: QCD- $WZjj$
- Parton-shower matching: VBF-H

## VBFNLO

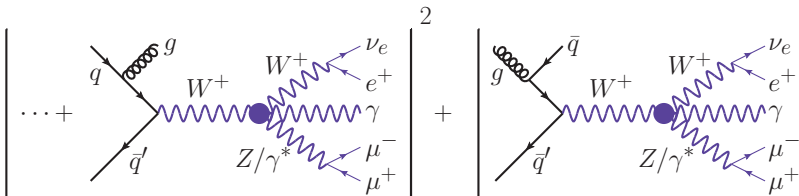
- Fully flexible parton-level Monte Carlo for processes with electroweak bosons
  - accurate predictions needed for LHC (both signal and background)
  - MC efficient solution for high number of final-state particles (decays of electroweak bosons included)
- general cuts and distributions of final-state particles
- various choices for renormalization and factorization scales
- any pdf set available from LHAPDF (or hard-wired CTEQ6L1, CT10, MRST2004qed, MSTW2008)
- event files in Les Houches Accord (LHA) or HepMC format (LO only)

## List of implemented processes

- vector-boson fusion production at **NLO QCD** of
  - Higgs (+**NLO EW, NLO SUSY**)
  - Higgs plus third hard jet
  - Higgs plus photon } (including Higgs decays)
  - vector boson ( $W, Z, \gamma$ )
  - two vector bosons ( $W^+W^-, W^\pm W^\pm, WZ, ZZ$ ;  $W\gamma$  will be in final VBFNLO 2.7.0)
- diboson production
  - diboson ( $WW, WZ, ZZ, W\gamma, Z\gamma, \gamma\gamma$ ) (**NLO QCD**)
  - diboson via gluon fusion ( $WW, ZZ, Z\gamma, \gamma\gamma$ )  
(part of **NNLO QCD contribution to diboson**)
  - diboson ( $WZ, W\gamma$ ) plus hard jet (**NLO QCD**)
- triboson production
  - triboson (all combinations of  $W, Z, \gamma$ ) (**NLO QCD**)
  - triboson ( $W\gamma\gamma$ ) plus hard jet (**NLO QCD**)
- Higgs plus two jets via gluon fusion (**one-loop LO**)  
(including Higgs decays)
- new physics models
  - anomalous Higgs couplings
  - anomalous triple and quartic gauge couplings
  - Higgsless and spin-2 models

Intermediate state Higgs boson in all processes included where applicable

- Helicity amplitude method [Hagiwara, Zeppenfeld]
- Same building blocks for different Feynman graphs
  - ⇒ Compute only once per phase-space point and reuse ("leptonic tensors")
  - Significantly faster than generated code (up to factor 10)



- Catani-Seymour dipole subtraction scheme

$$\sigma_{\text{NLO}} = \underbrace{\int_{m+1} [d\sigma^R|_{\epsilon=0} - d\sigma^A|_{\epsilon=0}]}_{\text{real emission}} + \underbrace{\int_m [d\sigma^V + \int_1 d\sigma^A]_{\epsilon=0}}_{\text{virtual contributions}} + \underbrace{\int_m d\sigma^C}_{\text{finite collinear term}}$$

- Photon isolation à la Frixione

Processes with real photons in final state can have configurations with photon collinear to final-state quark  $\rightarrow$  QED divergence

Simple (e.g.  $R$ ) separation cut between photon and jet not infrared safe  
 $\rightarrow$  Frixione photon isolation

$$\sum_i E_{T_i} \Theta(\delta - R_{i\gamma}) \leq p_{T\gamma} \frac{1 - \cos \delta}{1 - \cos \delta_0} \quad (\text{for all } \delta \leq \delta_0 = 0.7)$$

$\Rightarrow$  Efficiently suppresses fragmentation contribution

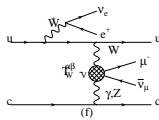
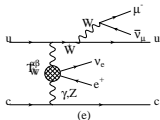
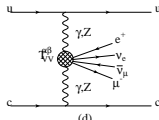
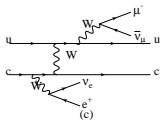
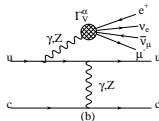
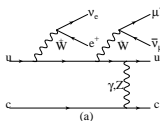
[Bozzi, Jäger, Oleari, Zeppenfeld; hep-ph/0603177, hep-ph/0604200, hep-ph/0701105]

[Denner, Hosekova, Kallweit ( $W^+W^+$ )]

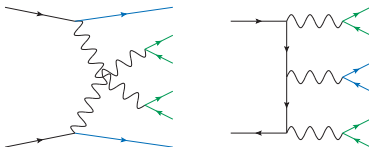
- Part of the NLO wishlist  
[Les Houches 2005]
- background to Higgs searches
- access to anomalous triple and quartic gauge couplings

Implementation:

- modular structure  
→ reuse building blocks
- leptonic decays included
- only t- and u-channel diagrams (s-channel implemented separately as triboson process)
- no interference effects from identical leptons

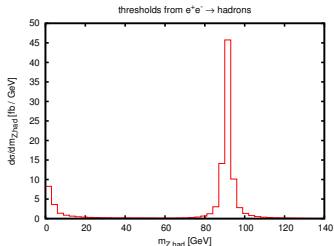
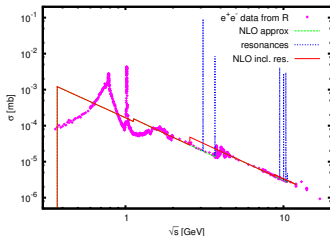


- Vector bosons have significant branching fractions into  $q\bar{q}$  final states  
 $BR(W \rightarrow q\bar{q}) \simeq BR(Z \rightarrow q\bar{q}) \simeq 70\%$
- $\Rightarrow$  Extend decay modes and let one vector boson decay hadronically
- $\Rightarrow$  semi-leptonic final states
- Vector-boson-fusion processes only contain t-channel exchange
- s-channel contribution can be viewed as triboson production with one vector boson decaying hadronically
- interference between s- and t-channel small  
 $\Rightarrow$  can be treated as separate process
- $\leftrightarrow$  s-channel contribution small in phenomenologically interesting phase-space regions ( $M_{jj,cut} \gg M_V$ )





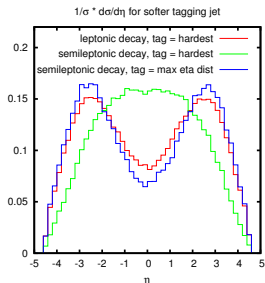
- Semileptonic decays implemented in the following channels:
  - $pp \rightarrow VVjj$  via VBF with  $VV \in W^+W^-, W^\pm W^\pm, W^\pm Z, ZZ$
  - $pp \rightarrow Hjj \rightarrow VVjj$  via VBF with  $VV \in W^+W^-, ZZ$
  - $pp \rightarrow VV$  with  $VV \in W^+W^-, W^\pm Z, ZZ$
  - $pp \rightarrow W^+W^-Z$  (other combinations will follow soon)
- Factor  $K = 1 + \frac{\alpha_s}{\pi}$  for  $V \rightarrow q\bar{q}$  decay can be added as NLO approximation for decay (assuming resonant  $V$  production dominates)
- Non-resonant contributions included
- Virtual photon decays  $\gamma^* \rightarrow q\bar{q}$ 
  - can form single jet in real emission part
  - quarks massless  $\Rightarrow$  divergence  $\leftrightarrow$  pion mass as regulator in reality
  - $\Rightarrow$  technical cut  $\rightarrow$  cross section depends on value
  - $\Rightarrow$  estimate size from  $e^+e^- \rightarrow$  hadrons without modelling resonances explicitly



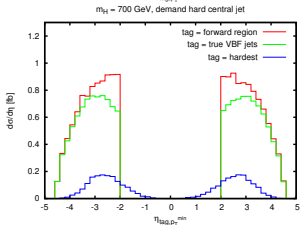
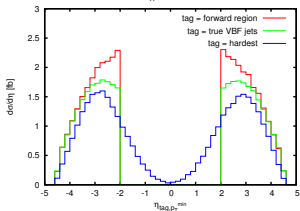
# Tagging jet definition

- two widely separated jets characteristic VBF signature
- leptonic decays: two hardest jets
- semileptonic decays: jet can come from vector boson decay  $\Rightarrow$  not a good choice
- alternatives:
  - two jets with largest distance in rapidity  $\rightarrow$  works for signal, but bad background rejection
  - separate phase space explicitly:
    - tagging jets:  $|\eta_{\text{tag}}| > \eta_c, \eta_1 \times \eta_2 < 0$
    - vector boson decay products:  $|\eta_{\text{decay}}| < \eta_c$
    - require high- $p_T$  jet in central region

$pp \rightarrow W^+ W^- jj$  via VBF, inclusive cuts



$pp \rightarrow H(\rightarrow W^+ W^-) jj$   
 $m_{H_1} = 700 \text{ GeV}$



# Anomalous quartic gauge couplings

Vector-boson scattering ideal process to test anomalous quartic gauge couplings

[New in VBFNLO 2.7.0beta: Feigl, Schlimpert]

Dimension-8 operators in Lagrangian

( $\Phi$  Higgs doublet,  $W^{\mu\nu}/B^{\mu\nu}$ : SU(2)/U(1) field strength tensors):

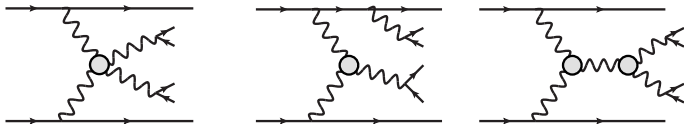
$$\mathcal{L}_{M,2} \propto [B^{\mu\nu} B_{\mu\nu}] \times \left[ (D^\beta \Phi)^\dagger D_\beta \Phi \right]$$

$$\mathcal{L}_{T,1} \propto [W^{\alpha\nu} W_{\mu\beta}] \times [W^{\mu\beta} W_{\alpha\nu}]$$

...

(at least) four gauge fields in each term  $\rightarrow$  modify quartic gauge couplings

triple gauge couplings contribute as well



Contribution of higher-dimensional operators can violate unitarity above certain energy scale  $\rightarrow$  **unphysical**

- Determine energy scale of unitarity violation  $\rightarrow$  Partial-wave analysis
    - Consider amplitudes for on-shell  $VV \rightarrow VV$  scattering ( $V \in W, Z, \gamma$ )
    - Decompose into series of partial waves with coefficients  $a_i, i = 0, 1, 2, \dots$
    - $\rightarrow$  Condition for unitarity conservation:  $|\text{Re}(a_i)| < \frac{1}{2}$
    - Strongest bound typically from  $i = 0 \rightarrow$  check only this contribution
- $\Rightarrow$  maximal energy scale  $\Lambda_{\text{max}}$
- Ensure unitarity at higher energies by applying form factor
    - Unitarity preserved by new-physics contributions entering at or before  $\Lambda_{\text{max}}$   
 $\rightarrow$  acts as cut-off
    - effective implementation in low-energy theory  $\Rightarrow$  form factor
    - explicit form model-dependent  $\rightarrow$  choice arbitrary
    - VBFNLO: dipole form factor

$$\mathcal{F}(s) = \frac{1}{\left(1 + \frac{s}{\Lambda_{\text{FF}}^2}\right)^n} \quad \Lambda_{\text{FF}}^2, n: \text{ free parameters}$$

- Determine maximal  $\Lambda_{\text{FF}}$  from given anomalous couplings,  $n$  and maximum energy considered

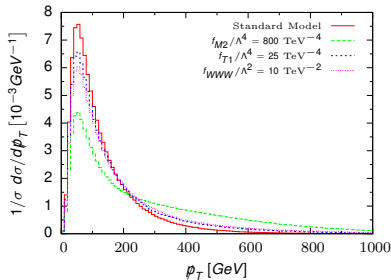
$\rightarrow$  implemented in form factor tool available from VBFNLO web site

<http://www.itp.kit.edu/~vbfnloweb/wiki/doku.php?id=download:formfactor>

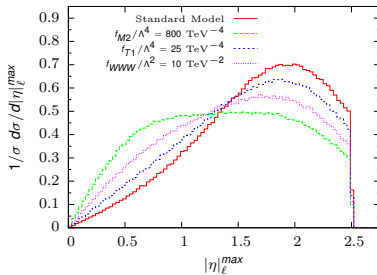
## Example output

```
[...]  
Reading in anomalous couplings parameter:  
  SQRT_S           = 14000.  
  FFEXP            = 2.0000  
  FS0              = 0.10000E-09  
  FS1              = 0.10000E-09  
[...]  
Checking tree-level unitarity violation with on-shell W+W- -> W+W- scattering  
using the largest helicity combination of the zeroth partial wave...  
[...]  
Checking tree-level unitarity violation with on-shell VV->VV scattering  
including all Q=0 channels involving W and Z bosons using the largest  
helicity combination of the zeroth partial wave...  
[...]  
Results for each channel, taking only the helicity combination with the largest  
contribution to the zeroth partial wave into account:  
  
FFscale_WWWW =      688. GeV    ( without FF: |Re(pwave_0)| > 0.5 at    0.8 TeV )  
[...]  
No tree-level unitarity violation in W+W- -> AA scattering found.  
[...]  
Results for each channel, taking contributions from all helicity combinations to  
the zeroth partial wave into account by diagonalizing the T-matrix:  
  
FFscale_WWWW_diag =      688. GeV    ( without FF: |Re(pwave_0)| > 0.5 at    0.8 TeV )  
[...]  
FFscale_VVVV_Q_0 =      622. GeV    ( without FF: |Re(pwave_0)| > 0.5 at    0.7 TeV )  
[...]
```

Normalized  $p_T$  distribution



Normalized  $|\eta|_\ell^{\max}$  distribution



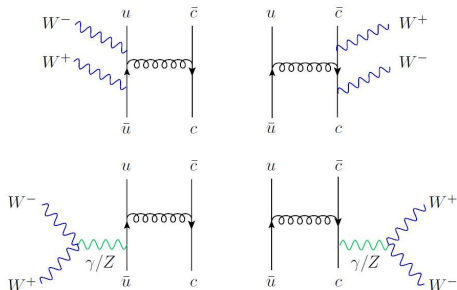
- Anomalous couplings enhance predominantly high-energy region
- $\Delta\sigma \sim \mathcal{O}(1 - 4\%)$  for total cross section,  
 $\Delta\sigma \sim \mathcal{O}(20 - 100\%)$  in high-energy region,  $m_{WW}^T > 800 \text{ GeV}$
- Visible changes in distributions, different for individual couplings
- $\rightarrow$  distinguish between different couplings

# QCD-Diboson production

$W^+ W^+ jj$  and  $W^+ W^- jj$  known at NLO QCD for some time

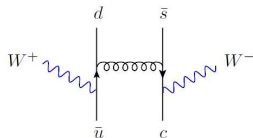
[Melia, Melnikov, Röntsch, Zanderighi; Greiner, Heinrich, Mastrolia, Ossola, Reiter, Tramontano]

$W^+ W^- jj$



$W^+ W^- jj$  &  $W^+ W^+ jj$

(latter after changing quark flavors appropriately)

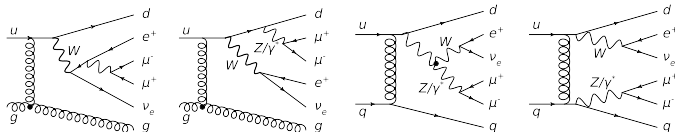


+ diagrams where quark line without attached vector bosons is replaced by gluons

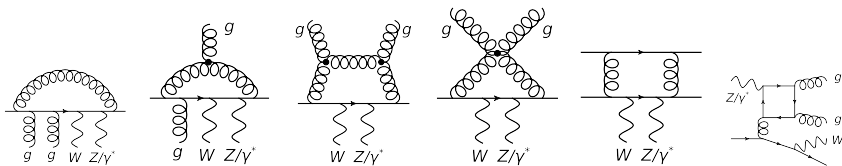
[Campanario, Kerner, Le, Zeppenfeld; will be in final VBFNLO 2.7.0]

QCD-induced WZjj production ( $\mathcal{O}(\alpha^4 \alpha_s^2)$ )

- Born: 90 subprocesses



- virtual corrections: up to rank-5 hexagons



- real emission: 146 subprocesses



# Speed comparison

## $W^+ Z_{jj}$ @ LO

runtime for 0.1% accuracy:

- VBFNLO: 8 min
- Sherpa: 5 h
- MadGraph 5: 1 month  
(based on extrapolation:  
0.7% in 14 hours)

## $W^+ Z_{jj}$ @ NLO

runtime for 1% accuracy:

- VBFNLO: 2-3 h

## Origin of better performance

- get rid of numerical instabilities
- combine and reuse similar contributions
- good phase-space generator

## $W^+ W^+ jj$ @ NLO

VBFNLO:

- 30 min for 1% accuracy

POWHEG-BOX:

- 200 jobs, 3 days each
- best result:  
8% accuracy
- median:  
60% accuracy
- worst result:  
off by factor  $10^6$   
(with error as large)
- combined result:  
1.1% (weighted mean)

$$pp \rightarrow e^+ \nu_e \mu^+ \mu^- jj, \sqrt{s} = 14 \text{ TeV}$$

- cuts

$$p_{T,j} > 20 \text{ GeV} \quad |\eta_j| < 4.5$$

$$p_{T,e} > 20 \text{ GeV} \quad |\eta_e| < 2.5$$

$$m_{e^+e^-} > 15 \text{ GeV} \quad \cancel{p}_T > 30 \text{ GeV}$$

$$R_{jj} > 0.4 \quad R_{\ell\ell} > 0.4$$

$$R_{j\ell} > 0.4$$

- PDF

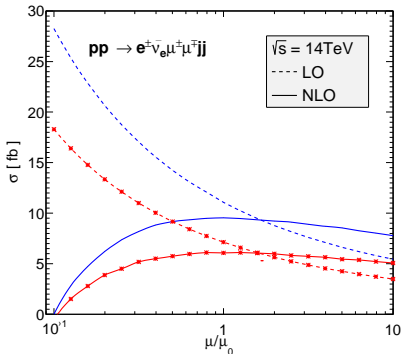
MSTW 2008 with  $n_F = 4$

- scale

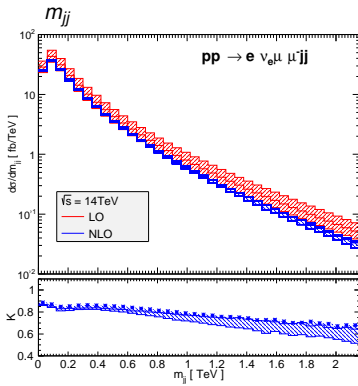
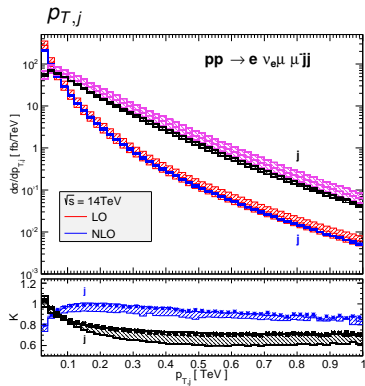
$$\mu = \mu_F = \mu_R$$

$$= \frac{1}{2} \left( \sum_{\text{jet}} p_{T,\text{jet}} + E_{T,W} + E_{T,Z} \right)$$

$$\text{with } E_{T,V} = \sqrt{p_{T,V}^2 + m_V^2}$$



→ scale dependence strongly reduced



→ Differential K factor varying in distributions

[New in VBFNLO 2.7.0 beta + upcoming Herwig++ release: Arnold et al.]

VBFNLO interfaced to Herwig++

requires some process-dependent modifications

⇒ currently only VBF-Higgs production, further processes will follow

→ Matching NLO calculations with parton shower

NLO calculation

- normalization correct to NLO
- additional jet at high- $p_T$  accurately described
- theoretical uncertainty reduced
- low- $p_T$  jet emission badly modelled
- parton level description

LO + parton shower

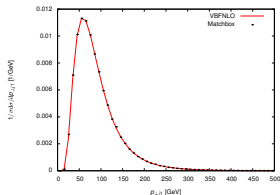
- LO normalization only
- further high- $p_T$  jets badly described
- Sudakov suppression at small  $p_T$
- events at hadron level possible

⇒ Herwig++ package Matchbox

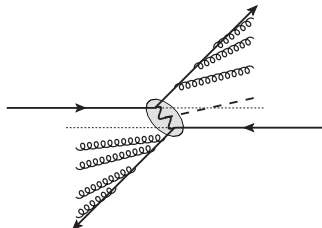
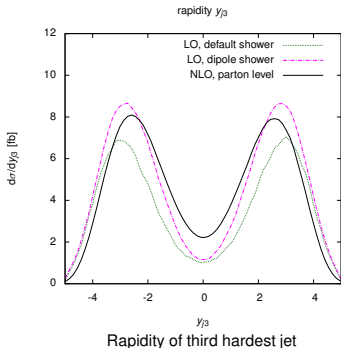
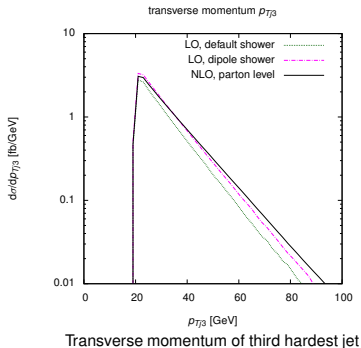
[Gieseke, Plätzer]

Parton shower based on Catani-Seymour dipoles

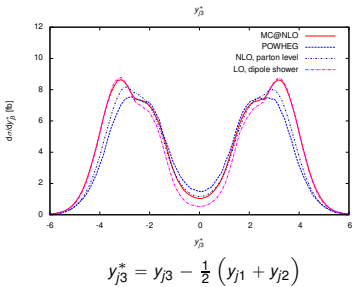
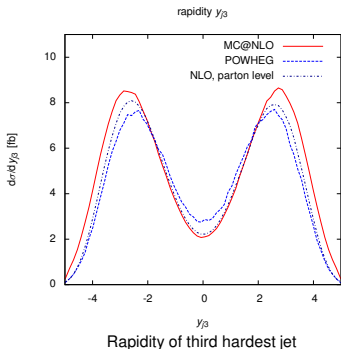
Matching methods: MC@NLO and POWHEG



NLO validation plot



- additional radiation by shower created mainly between jets and beam axis (color connections)
- dipole shower “interpolates” between NLO behavior in central region and shower behavior at small angles



- New features in VBFNLO
  - Semi-leptonic decays for  $VVjj$ ,  $VV$ ,  $WWZ$
  - Form factor tool
    - determine energy bound for unitarity violation in anomalous gauge couplings
    - calculate necessary form factor
- QCD- $WZjj$  at NLO QCD
  - fast implementation in VBFNLO
- Matching with parton shower

VBFNLO is a flexible parton-level Monte Carlo for processes with electro-weak bosons

Code available at

<http://www.itp.kit.edu/vbfnlo>

VBFNLO is collaborative effort:

K. Arnold, J. Bellm, G. Bozzi, M. Brieg, F. Campanario, C. Englert, B. Feigl, J. Frank, T. Figy, F. Geyer, N. Greiner, C. Hackstein, V. Hankele, B. Jäger, M. Kerner, G. Klämke, M. Kubocz, C. Oleari, S. Palmer, S. Plätzer, S. Prestel, MR, H. Rzehak, F. Schissler, O. Schlimpert, M. Spannowsky, M. Worek, D. Zeppenfeld

Contact: [vbfnlo@itp.kit.edu](mailto:vbfnlo@itp.kit.edu)