

QCD effects in vector-boson-fusion processes

Michael Rauch | April 25, 2016

INSTITUTE FOR THEORETICAL PHYSICS



Standard Model of Particle Physics

Status of a few years ago:

- matter particles: quarks, leptons
- force particles: photon, W/Z boson, gluon

mathematical description:

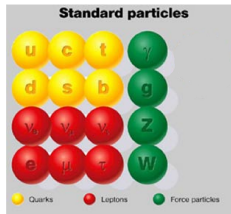
gauge theory ($SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$)

$$\mathcal{L} = \sum_L \bar{\psi}_L i \not{D}_L \psi_L + \sum_R \bar{\psi}_R i \not{D}_R \psi_R - \frac{1}{4} G_{\mu\nu}^a G^{a,\mu\nu} - \frac{1}{4} W_{\mu\nu}^a W^{a,\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu}$$

where

$$D_L^\mu = \partial^\mu + ig_s t^a G^{a,\mu} + ig' \frac{Y}{2} B^\mu - igt^a W^{a,\mu}$$

$$D_R^\mu = \partial^\mu + ig_s t^a G^{a,\mu} + ig' \frac{Y}{2} B^\mu$$



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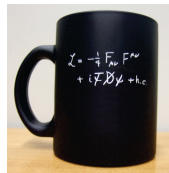
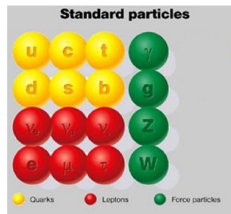
$$- \frac{1}{4} G_{\mu\nu}^a G^{a,\mu\nu} - \frac{1}{4} W_{\mu\nu}^a W^{a,\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu}$$

gluon
elektro-weak gauge bosons

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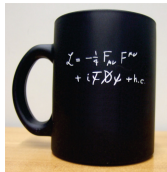
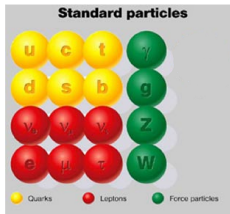
no mass terms fermion:

$$\mathcal{L}_{\text{mass},f} = -m_f (\bar{\psi}_L \psi_R + \bar{\psi}_R \psi_L)$$

gauge boson:

$$\mathcal{L}_{\text{mass},V} = -\frac{m_V^2}{2} V_\mu V^\mu$$

→ violate gauge invariance



Spontaneous Symmetry Breaking

Solution: spontaneous symmetry breaking

idea: additional field Φ such that \mathcal{L} invariant under gauge transformations
but ground state not invariant

\Rightarrow non-vanishing vacuum expectation value of Φ

Ex. ferro-magnetism:

$T > T_c$: no magnetisation \rightarrow rotational symmetry

$T < T_c$: spontaneous magnetisation \rightarrow preferred direction, symmetry broken

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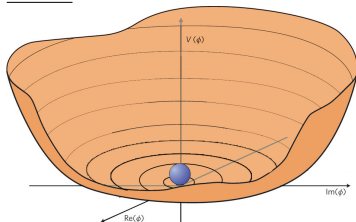
$T < T_c$: spontaneous magnetisation \rightarrow preferred direction, symmetry broken

field theory:

- global continuous symmetry:
massless Goldstone boson
for every broken generator
- local gauge symmetry:
eliminated by gauge transformations
(*would-be goldstone bosons*)
longitudinal modes of gauge bosons

$$\mathcal{L} \propto -\mu^2(\Phi^\dagger\Phi) - \lambda(\Phi^\dagger\Phi)^2$$

$$\mu^2 > 0$$



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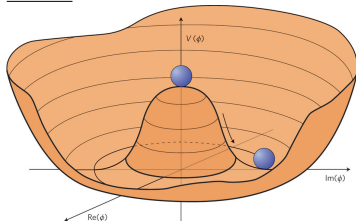
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Higgs Mechanism in the Standard Model

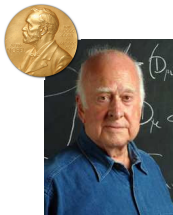
Standard Model: Higgs Mechanism

(based on similar ideas in solid state physics)

[Englert, Brout; Higgs; Guralnik, Hagen, Kibble 1964]

[Anderson 1963]

→ Nobel prize 2013



- Add Higgs field as $SU(2)$ doublet with hypercharge $+1$:

$$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}}(v + H + iG^0) \end{pmatrix}$$

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- Breaks $SU(2)_L \otimes U(1)_Y \rightarrow U(1)_{em}$ (\rightarrow photon massless)
- $G^\pm, G^0 \rightarrow$ longitudinal modes of W^\pm, Z
- H real scalar field \rightarrow Higgs boson

- $v = \frac{2M_W}{e\sqrt{1 - \frac{M_W^2}{M_Z^2}}} \simeq 246 \text{ GeV}$ vacuum expectation value

- Contribution to Lagrangian:

$$\mathcal{L}_H = (D_{L,\mu}\Phi)^\dagger (D_L^\mu\Phi)$$

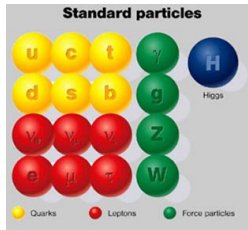
kinetic term

$$+ \frac{m_H^2}{2}\Phi^\dagger\Phi - \frac{m_H^2}{2v^2}(\Phi^\dagger\Phi)^2$$

Higgs potential

$$- (\lambda_\ell \bar{L}\Phi e_R + \lambda_u \bar{Q}\Phi^c u_R + \lambda_d \bar{Q}\Phi d_R + h.c.)$$

Yukawa coupling to fermions



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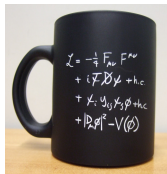
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- Contribution to Lagrangian:

$$\begin{aligned} \mathcal{L}_H &= (D_{L,\mu}\Phi)^\dagger (D_L^\mu\Phi) \\ &+ \frac{m_H^2}{2}\Phi^\dagger\Phi - \frac{m_H^2}{2v^2}(\Phi^\dagger\Phi)^2 \\ &- (\lambda_\ell \bar{L}\Phi e_R + \lambda_u \bar{Q}\Phi^c u_R + \lambda_d \bar{Q}\Phi d_R + h.c.) \\ &\stackrel{\text{SSB}}{=} \frac{1}{2}(\partial_\mu H)(\partial^\mu H) - \frac{m_H^2}{2}H^2 - \frac{m_H^2}{2v}H^3 - \frac{m_H^2}{8v^2}H^4 \\ &- (\text{mass and interaction terms with gauge bosons}) \\ &- \sum_{\text{fermions}} \frac{\lambda_f}{\sqrt{2}}(v + H)\bar{\psi}_f\psi_f \end{aligned}$$

↖ mass term ($m_f = \frac{\lambda_f v}{\sqrt{2}}$)
 ↖ fermion-Higgs coupling



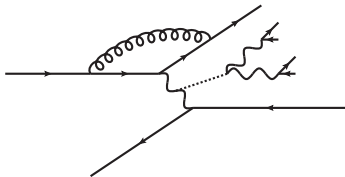
- **Lagrangian** defines all fundamental fields and interactions
- Seven particle types hit (LHC) detector elements:
 $p, n, \pi, K, e, \mu, \gamma$
- \leftrightarrow **direct** calculation practically not possible
final-state multiplicity, non-perturbative effects, . . .
- \rightarrow **Monte Carlo Event Generators**

evolution from hard process down to hadron level

Major generators:

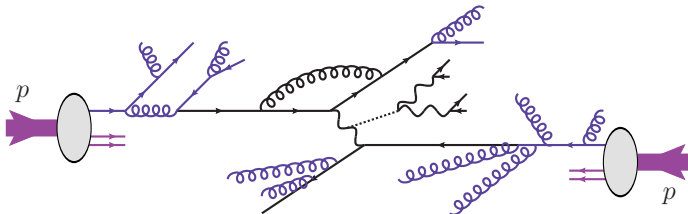
- Pythia [Sjöstrand]
- Sherpa [Krauss et al.]
- Herwig [Bellm, Gieseke, Grellscheid, Plätzer, MR, Reuschle, Richardson, Schichtel, Seymour, Siodmok, Wilcock, Fischer, Harrendorf, Nail, Papaefstathiou, D. Rauch]
- . . .

Hard Process



- calculable by perturbation theory
- LO / NLO QCD / NLO QCD+EW accuracy
- typical scale $\mathcal{O}(100 \text{ GeV})$

Parton Shower

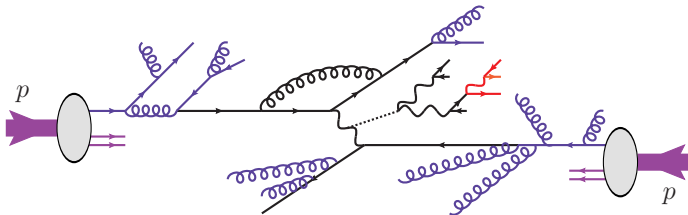


- initial- and final-state parton shower
- based on **unitarity** and **collinear factorization**
- adds **additional radiation** according to DGLAP splitting kernels P
- evolution governed by **Sudakov factor**
(non-emission probability between hard scale θ_{\max} and probed scale θ)

$$\Delta(\theta_{\max}, \theta) = \exp \left(- \sum_j \int_{\theta^2}^{\theta_{\max}^2} \frac{d\tilde{\theta}^2}{\tilde{\theta}^2} \int_{z_-(\tilde{\theta})}^{z_+(\tilde{\theta})} dz \frac{\alpha_S}{2\pi} P_{ij}(z) \right)$$

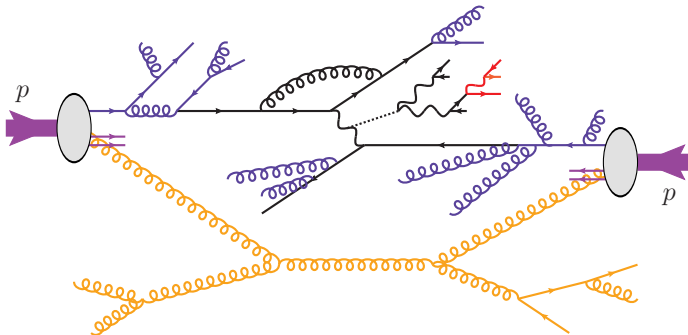
- resums leading logs and in large- N limit also next-to-leading logs
- evolution stops at $\mathcal{O}(1 \text{ GeV})$
→ α_S large, perturbative expansion breaks down

Perturbative Decays of Heavy Particles



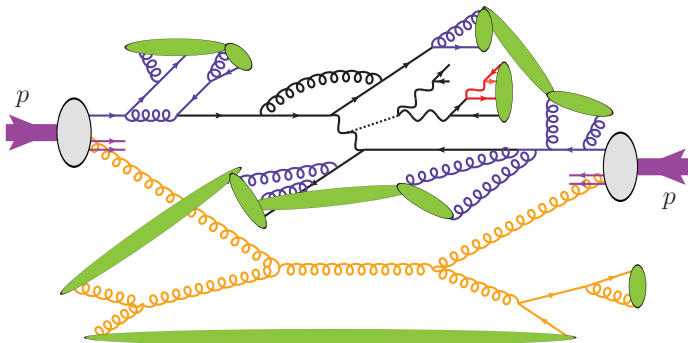
- simulate decays of any remaining heavy particles, e.g. t , W , Z , H

Secondary Hard Processes



- proton remnants can scatter again
→ multi-parton interactions (MPI)
- another proton from bunch can scatter as well
→ pile-up
- Poisson statistics
- mostly QCD $2 \rightarrow 2$ processes, dominated by t-channel gluon exchange

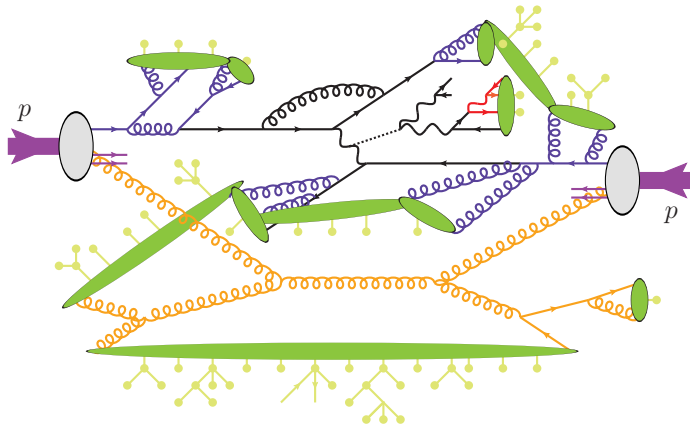
Hadronization



- re-group partons into (colourless) hadrons
- phenomenological model
- parameters fitted from experimental data

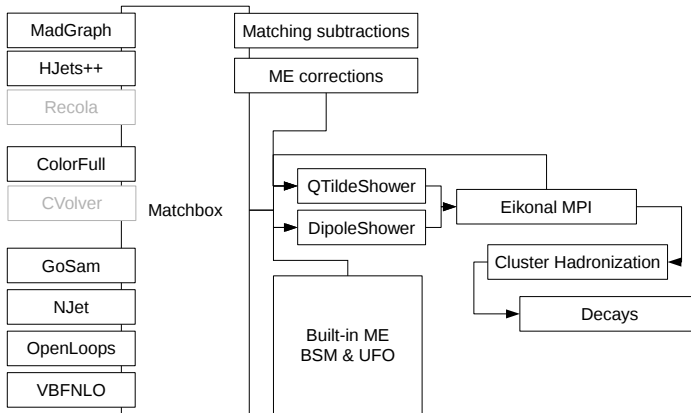
Monte Carlo Event (6)

Hadron Decays



- Decay unstable hadrons to final set

- fully automated matching of NLO to parton showers through Matchbox module
[J. Bellm, S. Plätzer, MR, C. Reuschle, A. Wilcock]
- subtractive (MC@NLO-type, \oplus) and multiplicative (POWHEG-type, \otimes) matching
- angular-ordered (QTilde, PS) and dipole (Dipoles) shower
- matrix elements through binary interface, no event files



VBF event topology

VBF (vector-boson fusion) topology shows distinct signature

- two tagging jets in forward region
- reduced jet activity in central region
- leptonic decay products typically between tagging jets

→ two-sided DIS

First studied in context of Higgs searches [Han, Valencia, Willenbrock; Fgy, Oleari, Zeppenfeld; ...]

- ~ 10% compared to main production mode gluon fusion
- NLO QCD corrections moderate ($\mathcal{O}(\lesssim 10\%)$)
- NLO EW same size, opposite sign as QCD for $M_H \sim 126$ GeV

[Ciccolini *et al.*, Fgy *et al.*]

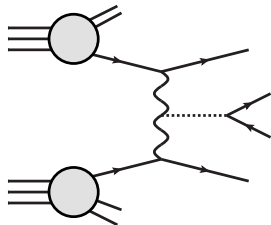
- NNLO QCD known for subsets: no significant contributions for integrated c.s.

[Harlander *et al.*, Bolzoni *et al.*]

corrections up to 10% in distributions

[Cacciari *et al.*]

- advantageous scale choice: momentum transfer q^2 of intermediate vector bosons



[Bozzi, Jäger, Oleari, Zeppenfeld (VV); Campanario, Kaiser, Zeppenfeld ($W^\pm \gamma$)]

[Denner, Hosekova, Kallweit (W^+W^+)]

- Important process for LHC run-II
- Part of the NLO wish list

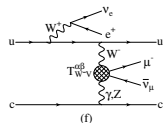
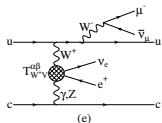
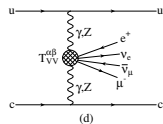
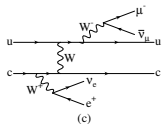
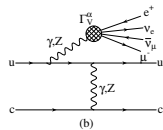
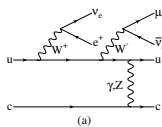
[Les Houches 2005]

- background to Higgs searches
- access to anomalous triple and quartic gauge couplings

- NLO QCD implementation of

- all boson combinations
- leptonic and semi-leptonic decays
- including off-shell and non-resonant contributions
- VBF approximation

→ **VBFNLO** [MR, Zeppenfeld et al.]



NLO plus Parton Shower

Combine advantages of NLO calculations and parton shower

NLO calculation

- normalization correct to NLO
- additional jet at high- p_T accurately described
- theoretical uncertainty reduced

Parton shower

- Sudakov suppression at small p_T
- events at hadron level possible

State of the Art

Implementations for specific VBF processes

- POWHEG-BOX

[Alioli, Hamilton, Nason, Oleari, Re]

currently available VBF implementations:

Z [Jäger, Schneider, Zanderighi]

W^\pm, Z [Schissler, Zeppenfeld]

$W^\pm W^\pm, W^\pm W^\mp$ [Jäger, Zanderighi]

ZZ [Jäger, Karlberg, Zanderighi]

- VBF- H with POWHEG method

[D'Errico, Richardson]

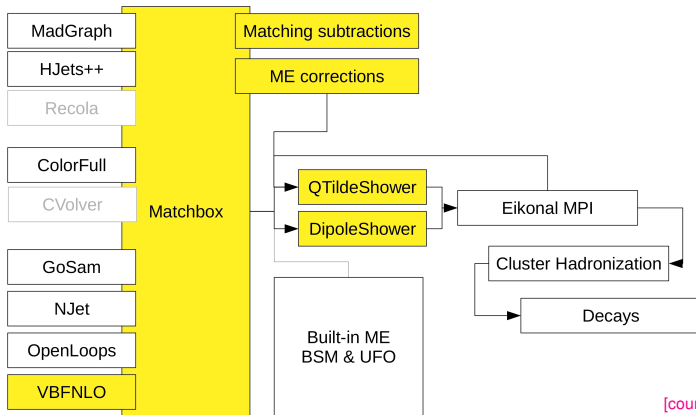
- HJets++

[Campanario, Figy, Plätzer, Sjödalh]

→ process-by-process implementation → **slow** progress on **availability**

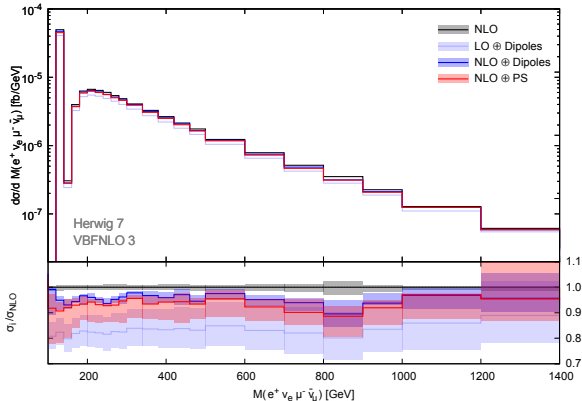
VBFNLO 3 & Herwig 7 – this talk

- matrix elements from VBFNLO via **BLHA2** interface
→ **all combinations** including leptonic gauge-boson decays
- extensions to make accessible
 - phase-space sampling
 - (electroweak) random helicity summation
 - anomalous couplings



[courtesy of S. Plätzer]

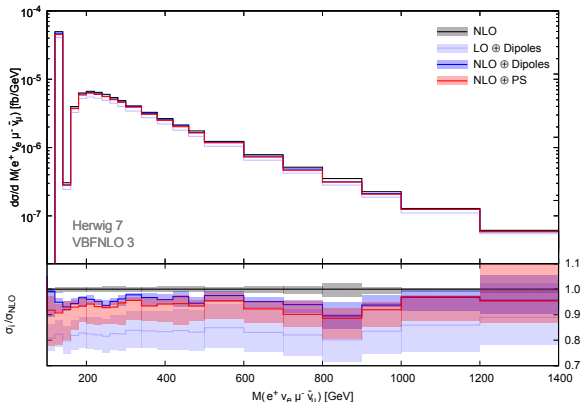
Process as example: $pp \rightarrow ((Hjj \rightarrow) W^+ W^- jj \rightarrow) e^+ \nu_e \mu^- \bar{\nu}_\mu jj$ via VBF
 Four-lepton invariant mass



- Higgs peak at 125 GeV
- WW continuum production above 180 GeV
- significant cancellation between diagrams at high invariant masses
- \Rightarrow ideal test for anomalous couplings

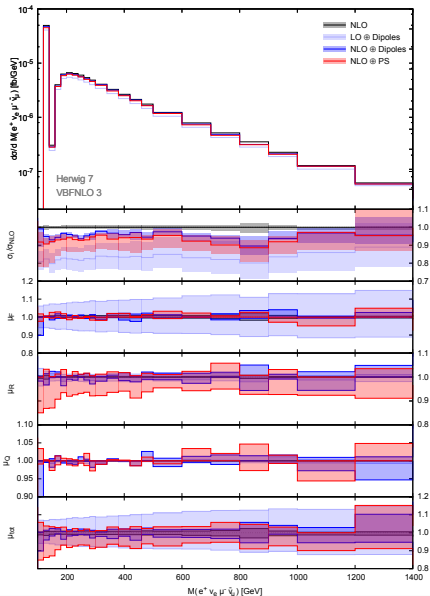
Distributions

Process as example: $pp \rightarrow ((Hjj \rightarrow) W^+ W^- jj \rightarrow) e^+ \nu_e \mu^- \bar{\nu}_\mu jj$ via VBF
 Four-lepton invariant mass



- all parton-shower results smaller than NLO cross section
- additional parton splittings hard, wide-angle \rightarrow separate jet
- \leftrightarrow VBF cut $m_{jj} > 600$ GeV
- no relevant shape changes (as expected: insensitive to QCD effects)

Four-lepton Invariant Mass



← central scale $\mu_0 = p_{T,j1}$
transverse momentum of
leading jet

← band: scale variation
 $\{\mu_F, \mu_R, \mu_Q\} / \mu_0 \in [\frac{1}{2}; 2]$
 $\mu_i / \mu_j \in [\frac{1}{2}; 2]$

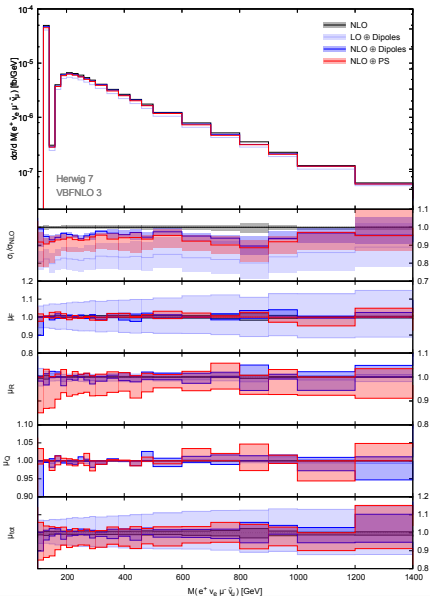
← factorization scale
 $\mu_F \in [\frac{1}{2}; 2]$

← renormalization scale
 $\mu_R \in [\frac{1}{2}; 2]$

← shower scale
 $\mu_Q \in [\frac{1}{2}; 2]$

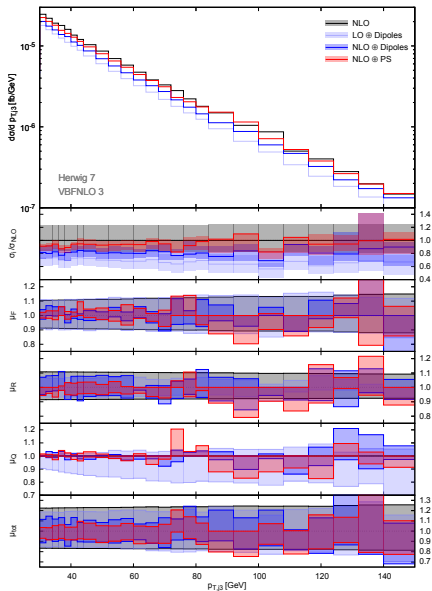
← all three scales

Four-lepton Invariant Mass



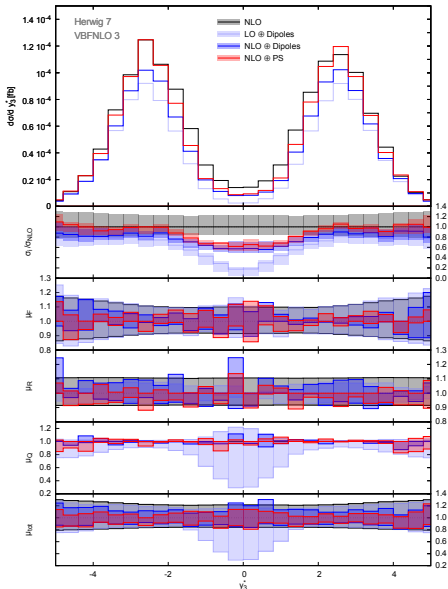
- consistent variation of scales between hard process and parton shower
- large factorization scale dependence for LO result
- larger dependence for down variation of renormalization scale in angular-ordered shower:
↔ under investigation
- small variations from shower-scale changes
- modest remaining overall uncertainty

Transverse Momentum Third Jet



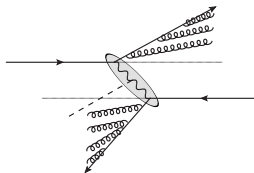
- large scale variation bands for
 - shower scale in LO ⊕ Dipoles
 - pure parton-shower effect
 - fact./ren. scale in “NLO”
 - LO accuracy of observable
- reduced for both NLO + parton-shower curves
- still significant remaining uncertainty $\mathcal{O}(10 - 20\%)$
- → call for multi-jet merging

Rapidity of third jet



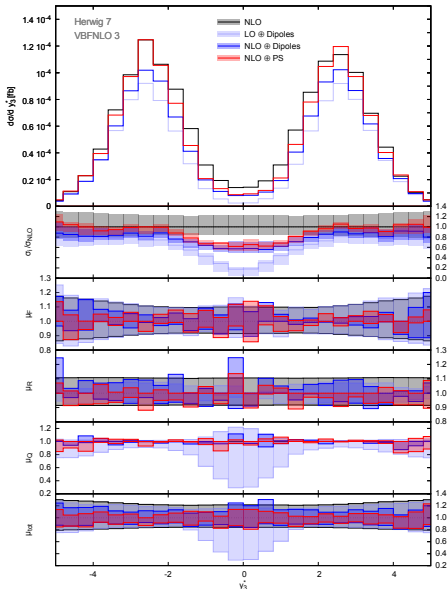
Rapidity of third jet relative to two tagging jets

$$y_3^* = y_3 - \frac{y_1 + y_2}{2}$$



- VBF colour structure suppresses additional central jet radiation
- colour connection between tagging jet and remnant
- ↔ distinction from QCD-induced production

Rapidity of third jet

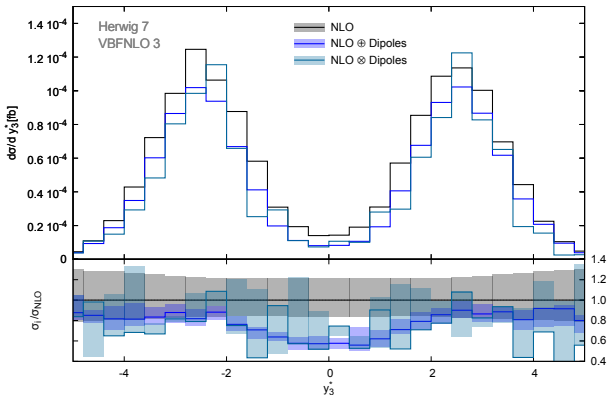


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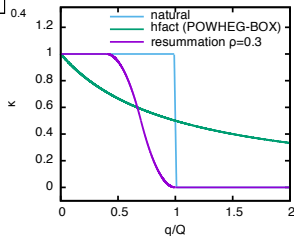
- impact of parton showers (+LO) long unclear
- Herwig predicts very low radiation in central region
- large shower-scale unc.
- stabilised when combining with NLO
- still reduction present
- scale variation bands not overlapping
- only small effects in forward region (mostly global normalization)

Rapidity of third jet – POWHEG

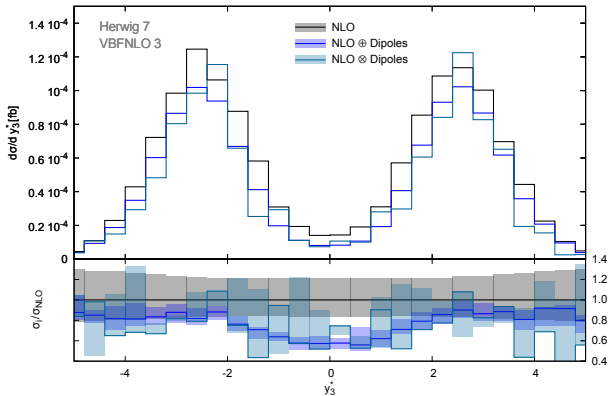


- POWHEG-like (\otimes) using resummation scheme [Plätzer]:

$$\kappa(Q, q; \rho) = \begin{cases} 1 & \text{for } q < (1 - 2\rho)Q \\ 1 - \frac{(1 - 2\rho - \frac{q}{Q})^2}{2\rho^2} & \text{for } (1 - 2\rho)Q < q < (1 - \rho)Q \\ \frac{(1 - \frac{q}{Q})^2}{2\rho^2} & \text{for } (1 - \rho)Q < q < Q \\ 0 & \text{for } q > Q \end{cases}$$



Rapidity of third jet – POWHEG



- band: joint variation $\mu_F = \mu_R = \mu_Q \in [\frac{1}{2}, 2] \mu_0$
- similar predictions from MC@NLO-like (\oplus) and POWHEG-like (\otimes) matching
- also holds for other distributions

Effective Field Theory

Assumption: new physics is heavy

Classic example: μ decay \rightarrow Fermi theory (t-channel W integrated out)



$$G_F = \frac{\sqrt{2}}{8} \frac{g^2}{m_W^2}$$

\Rightarrow Effective Lagrangian

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} + \sum_{d>4} \sum_i \frac{f_i^{(d)}}{\Lambda^{d-4}} \mathcal{O}_i^{(d)}$$

- operators \mathcal{O} contain SM fields only
- respect SM gauge symmetries
- suppressed by $1/\Lambda^{d-4}$ (Λ : scale of new physics)
 \rightarrow keep only leading order (lowest dimension $d = 6$)
- building blocks:
 - Higgs field Φ
 - (covariant) derivative ∂^μ, D^μ
 - field strength tensors $G^{\mu\nu}, W^{\mu\nu}, B^{\mu\nu}$
 - fermion fields ψ

Unitarity Violation

Important gauge **cancellations** between different diagram types

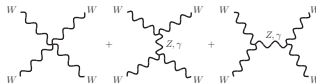
- longitudinal W scattering through quartic gauge boson vertex



high energy limit: centre-of-mass energy $\sqrt{s} \rightarrow \infty$

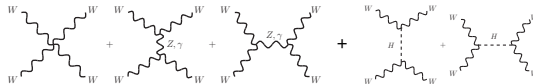
$$\mathcal{M}_{\text{quartic vertex}} \propto s^2 \rightarrow \text{cross section diverges} \quad \sigma \propto s^4 \rightarrow \infty$$

- add triple gauge boson vertices



$\mathcal{M}_{\text{quartic vertex}} \propto s \rightarrow$ still **divergent**

- additional Higgs diagrams



remove divergence exactly $\sigma \propto 1/S \rightarrow 0$

Anomalous gauge couplings spoil cancellation \rightarrow stringent **tests**

Anomalous gauge couplings spoil cancellation
 \leftrightarrow effects can become large \rightarrow **unitarity violation**

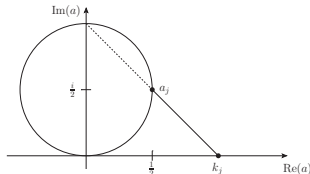
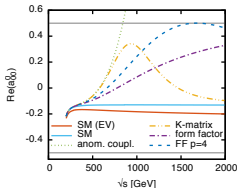
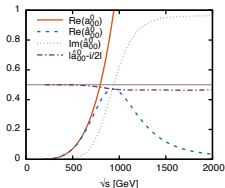
Several solutions:

- consider only unitarity-conserving phase-space regions
 throws away information \rightarrow reduced sensitivity
- (dipole) **form factor** multiplying amplitudes

$$\mathcal{F}(s) = \frac{1}{\left(1 + \frac{s}{\Lambda_{\text{FF}}^2}\right)^n}$$

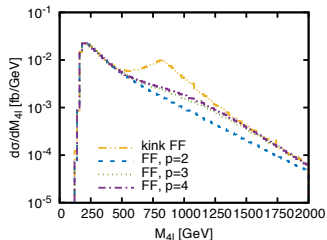
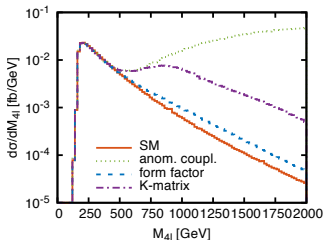
Λ_{FF}^2 , n : free parameters

- **K-matrix unitarization** [Alboteanu, Kilian, Reuter, Sekulla]
 based on partial-wave analysis [Jacob, Wick]
 project amplitude back onto **Argand circle**



Cross Section Results

Example Process: $pp(\rightarrow W^+W^+jj) \rightarrow e^+\nu_e\mu^+\nu_\mu jj$ at NLO QCD accuracy



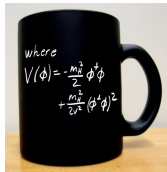
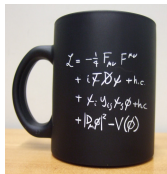
- kink form factor (simplified projection for comparison):

$$F_{\text{kink}}(E) = \begin{cases} 1 & \text{for } E \leq \Lambda_{\text{FF,kink}} , \\ \left(\frac{\Lambda_{\text{FF,kink}}}{E}\right)^4 & \text{for } E > \Lambda_{\text{FF,kink}} , \end{cases}$$

- huge effects for un-unitarized result \leftrightarrow **unphysical**
- *K*-matrix method maximising contribution while staying in physical region
- \rightarrow study parton-shower and hadronization impact

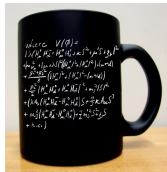
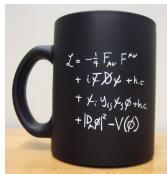
Parton-shower and scale variation effects in
 $W^+ W^- jj$ production via vector-boson-fusion

- **important** process for the LHC
 - Higgs properties – unitarity in WW scattering
 - testing anomalous (triple and) quartic gauge couplings
- study performed with **Herwig 7** & **VBFNLO 3**
- **compatible** behavior of both parton showers and matching schemes
- **small** parton-shower effects for distributions of variables already present at LO
 - mostly reduction of inclusive cross section due to additional jet radiation
- presence of **central rapidity gap stabilised**
- → study **hadronization** impact



Parton-shower and scale variation effects in
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Cuts:

$$\begin{aligned} p_{T,j} &> 30 \text{ GeV}, & |y_j| &< 4.5, \\ p_{T,\ell} &> 20 \text{ GeV}, & |y_\ell| &< 2.5, \\ m_{j_1,j_2} &> 600 \text{ GeV}, & |y_{j_1} - y_{j_2}| &> 3.6, \end{aligned}$$

(inspired from ATLAS VBF category in $H \rightarrow WW$, CMS similar)

Defined standardized interface between Monte Carlo tools and one-loop programs

→ [Binoth Les Houches Accord \(BLHA\)](#)

[[arXiv:1001.1307](#), [arXiv:1308.3462](#)]

- tree-level evaluation of matrix elements well under control
- modular structure of NLO calculations
- algorithms for treatment of infrared singularities (Catani-Seymour, FKS, ...)
- → incorporate one-loop matrix element information into MC tools

Distribution of tasks:

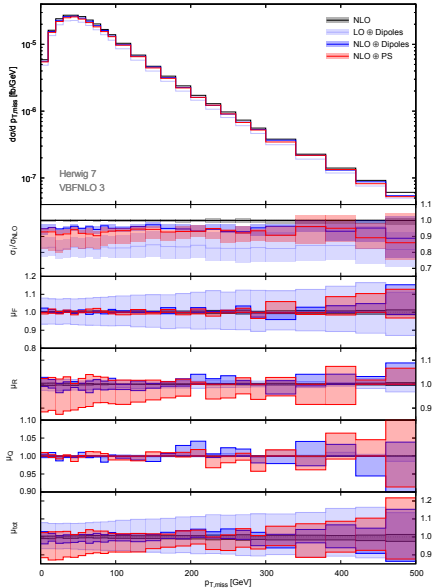
- MC tool:
 - cuts, histograms, parameters
 - Monte Carlo integration
 - phase space (→ [VBFNLO](#))
 - IR subtraction
 - Born, colour- and spin-correlated Born ([only BLHA1](#))
- One-loop provider (OLP):
 - one-loop matrix elements $2\Re(\mathcal{M}_{\text{LO}}^\dagger \mathcal{M}_{\text{virt}})$ (coefficients of ϵ^{-2} , ϵ^{-1} , ϵ^0 ; $|\mathcal{M}_{\text{LO}}|^2$)
 - Born, colour- and spin-correlated Born ([only BLHA2](#))

Setup stage via “contract” file

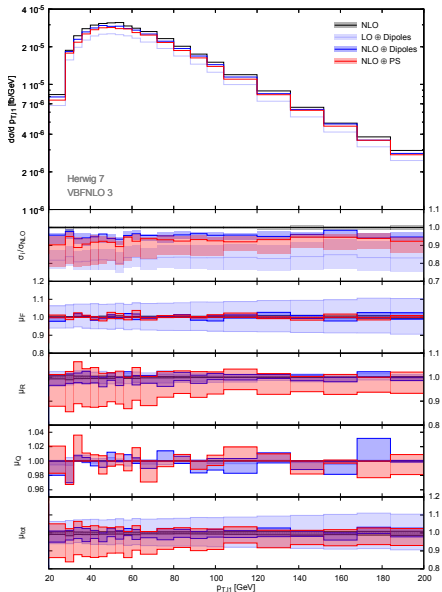
(needed for tools which generate code on the fly)

Run-time stage via binary interface (function calls) → fast

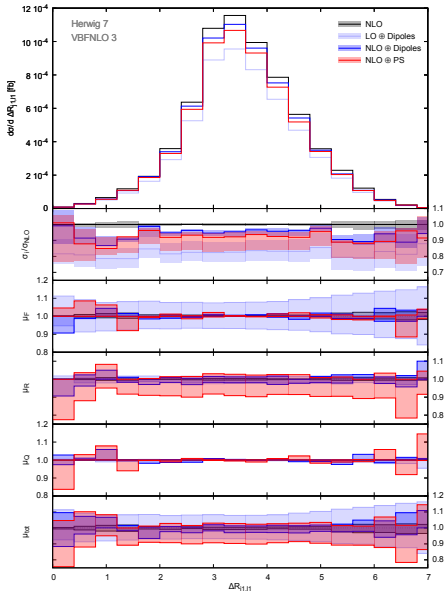
Missing Transverse Momentum



Transverse Momentum of Leading Lepton



R Separation of Leading Jet and Leading Lepton



$$\Delta R = \sqrt{\Delta y^2 + \Delta \phi^2}$$

Jacobian peak at $\Delta R_{j1l1} = \pi$