

Vector-Boson-Fusion: Parton-shower and Anomalous-coupling Effects

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INSTITUTE FOR THEORETICAL PHYSICS



VBF event topology

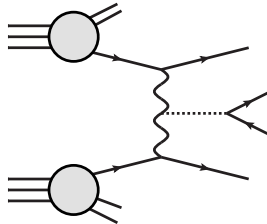
VBF (vector-boson fusion) topology shows distinct signature

- two tagging jets in forward region
- reduced jet activity in central region
- leptonic decay products typically between tagging jets

→ two-sided deep-inelastic scattering

First studied in context of Higgs searches [Han, Valencia, Willenbrock; Figy, Oleari, Zeppenfeld; ...]

- $\sim 10\%$ compared to main production mode gluon fusion
- NLO QCD corrections moderate ($\mathcal{O}(\lesssim 10\%)$)
- NLO EW same size [Ciccolini *et al.*, Figy *et al.*]
- NNLO QCD known for subsets:
no significant contributions for integrated c.s.
[Harlander *et al.*, Bolzoni *et al.*]
corrections up to 10% in distributions [Cacciari *et al.*]
- incl. NNNLO QCD: tiny effects [Dreyer, Karlberg]
- advantageous scale choice:
momentum transfer q^2 of intermediate vector bosons



[Bozzi, Jäger, Oleari, Zeppenfeld (VV); Campanario, Kaiser, Zeppenfeld ($W^\pm \gamma$)]

[Denner, Hosekova, Kallweit (W^+W^+)]

- Important process for LHC run-II
- Part of the NLO wish list

[Les Houches 2005]

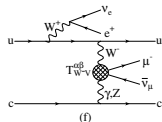
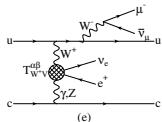
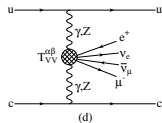
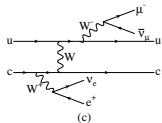
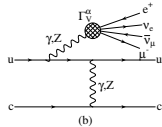
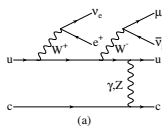
- background to Higgs searches
- access to anomalous triple and quartic gauge couplings

- NLO QCD implementation of

- all boson combinations
- leptonic and semi-leptonic decays
- including off-shell and non-resonant contributions
- VBF approximation

→ VBFNLO

[MR, Zeppenfeld et al.]



VBFNLO

Vector-Boson-Fusion at Next-to-Leading Order

VBFNLO

Physics
Vector-Boson-Fusion at Next-to-Leading Order

VBFNLO

F
Physics

Vector-Boson-Fusion at Next-to-Leading Order

- Fully flexible parton-level Monte Carlo for processes with electroweak bosons
 - accurate predictions needed for LHC (both signal and background)
 - MC efficient solution for high number of final-state particles (decays of electroweak bosons included)
- general cuts and distributions of final-state particles
- various choices for renormalization and factorization scales
- any pdf set available from LHAPDF (or hard-wired CTEQ6L1, CT10, MRST2004qed, MSTW2008)
- event files in Les Houches Accord (LHA) or HepMC format (LO only)
- BLHA interface to Monte-Carlo event generators
→ NLO event output

List of implemented processes

(New in VBFNLO 2.7.1/3.0.0 β 1)

- vector-boson fusion production at **NLO QCD** of
 - Higgs (+**NLO EW**, **NLO SUSY**)
 - Higgs plus third hard jet
 - Higgs plus photon
 - Higgs pair} (including Higgs decays)
 - vector boson (W, Z, γ)
 - two vector bosons ($W^+W^-, W^\pm W^\pm, WZ, ZZ, W\gamma, Z\gamma$)
- diboson production
 - diboson ($WW, WZ, ZZ, W\gamma, Z\gamma, \gamma\gamma$) (**NLO QCD**)
 - diboson via gluon fusion ($WW, ZZ, Z\gamma, \gamma\gamma$) (part of **NNLO QCD** contribution to diboson)
 - diboson ($WW, WZ, ZZ, W\gamma$) plus hard jet (**NLO QCD**)
 - diboson ($W^\pm W^\pm, WZ, W\gamma, ZZ, Z\gamma$) plus two hard jets (**NLO QCD**)
- triboson production (**NLO QCD**)
 - triboson (all combinations of W, Z, γ)
 - triboson ($W\gamma\gamma$) plus hard jet
- Higgs plus vector boson (**NLO QCD**) (including Higgs decays)
 - Higgs plus vector boson (WH)
 - Higgs plus vector boson plus hard jet (WH)
- Higgs plus two jets via gluon fusion (**one-loop LO**) (including Higgs decays)
- new physics models
 - anomalous Higgs, triple and quartic gauge couplings
 - **K-matrix unitarization for selected couplings**
 - Higgsless and spin-2 models
 - Two-Higgs model
- **BLHA interface for VBF processes**

Combine advantages of NLO calculations and parton shower

NLO calculation

- normalization correct to NLO
- additional jet at high- p_T accurately described
- theoretical uncertainty reduced

Parton shower

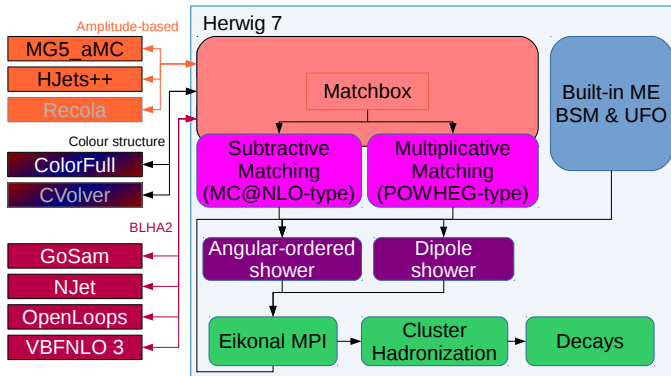
- Sudakov suppression at small p_T
- events at hadron level possible

State of the Art

Implementations for specific VBF processes

- POWHEG-BOX [Alioli, Hamilton, Nason, Oleari, Re]
currently available VBF implementations:
 - Z [Jäger, Schneider, Zanderighi]
 - W^\pm, Z [Schissler, Zeppenfeld]
 - $W^\pm W^\pm, W^\pm W^\mp$ [Jäger, Zanderighi]
 - ZZ [Jäger, Karlberg, Zanderighi]
- VBF- H with POWHEG method [D'Errico, Richardson]
- HJets++ [Campanario, Figy, Plätzer, Sjödalh]

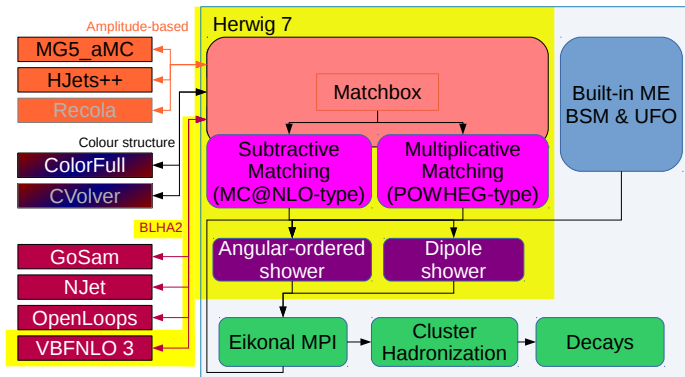
- fully automated matching of NLO to parton showers through Matchbox module
[work led by S. Plätzer with substantial contributions by J. Bellm, A. Wilcock, MR, C. Reuschle]
- subtractive (MC@NLO-type, \oplus) and multiplicative (POWHEG-type, \otimes) matching
- angular-ordered (QTilde, **PS**) and dipole (**Dipoles**) shower
- matrix elements through binary interface, no event files



VBFNLO 3 & Herwig 7 – this talk

- matrix elements from VBFNLO via **BLHA2** interface
- extensions to make accessible
 - phase-space sampling
 - (electroweak) random helicity summation
 - anomalous couplings

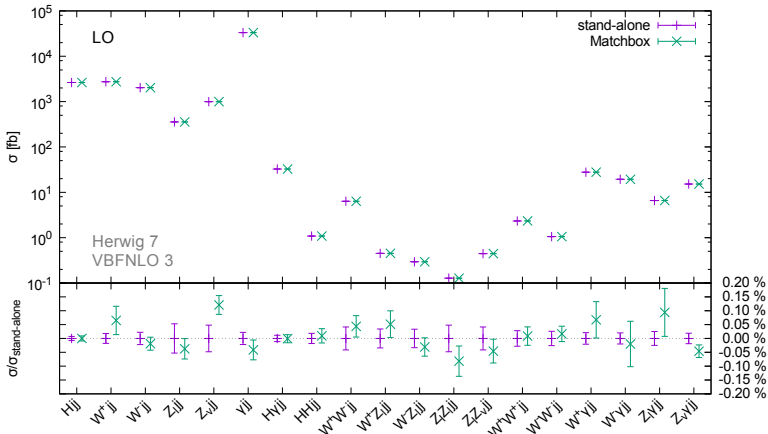
[Binoth et al., Alioli et al.]



Validation

Compare LO results between VBFNLO stand-alone run and interfaced to Herwig 7 via Matchbox

(inclusive cuts, with leptonic gauge boson decays into single different-flavour combination, Higgs non-decaying)

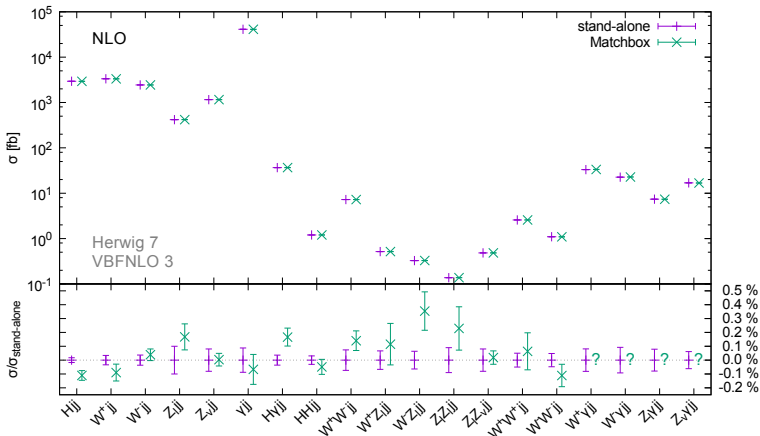


→ good agreement at or below permill level

Validation

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→ good agreement

$V\gamma$ processes: $\pm 0.7\%$ deviation \leftrightarrow beyond errors → under investigation

Process:

$$pp \rightarrow ((Hjj \rightarrow)W^+W^-jj \rightarrow)e^+\nu_e\mu^-\bar{\nu}_\mu jj \text{ via VBF}$$

Cuts:

$$\begin{aligned} p_{T,j} &> 30 \text{ GeV}, & |y_j| &< 4.5, \\ \text{anti-}k_T \text{ jets with } R &= 0.4, & & b\text{-quark veto} \end{aligned}$$

$$\begin{aligned} p_{T,\ell} &> 20 \text{ GeV}, & |y_\ell| &< 2.5, \\ m_{e^+,\mu^-} &> 15 \text{ GeV}, & & \end{aligned}$$

$$m_{j_1,j_2} > 600 \text{ GeV}, \quad |y_{j_1} - y_{j_2}| > 3.6$$

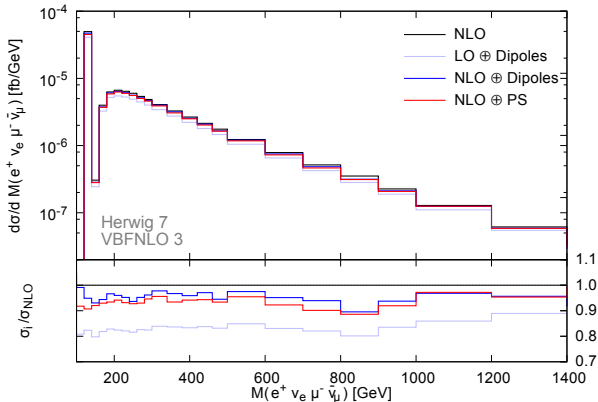
(inspired from ATLAS VBF category in $H \rightarrow WW$, CMS similar)

PDF: MMHT2014

central scale choice: transverse momentum of the leading jet

$$\mu_0 = p_{T,j_1}$$

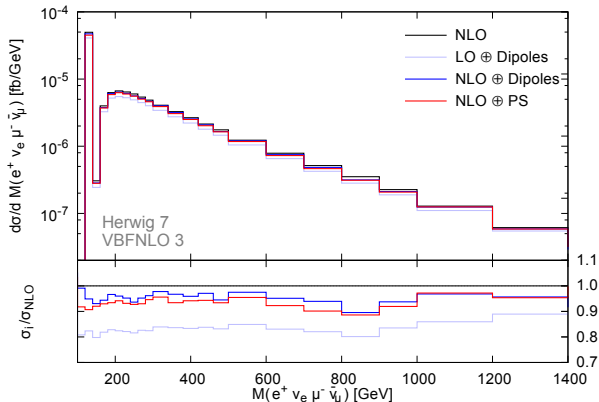
Process as example: $pp \rightarrow ((Hjj \rightarrow) W^+ W^- jj \rightarrow) e^+ \nu_e \mu^- \bar{\nu}_\mu jj$ via VBF
 Four-lepton invariant mass



- Higgs peak at 125 GeV
- WW continuum production above 180 GeV
- significant cancellation between diagrams at high invariant masses
- \Rightarrow ideal test for anomalous couplings

Distributions

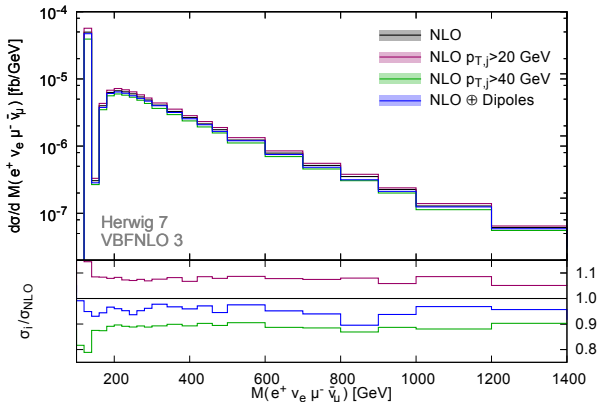
Process as example: $pp \rightarrow ((Hjj \rightarrow) W^+ W^- jj \rightarrow) e^+ \nu_e \mu^- \bar{\nu}_\mu jj$ via VBF
Four-lepton invariant mass



- all parton-shower results smaller than NLO cross section
- additional K -factor effect for LO ⊕ Dipoles result ($K = 1.077$)
- no relevant shape changes
(as expected: insensitive to QCD effects)

Migration Effects

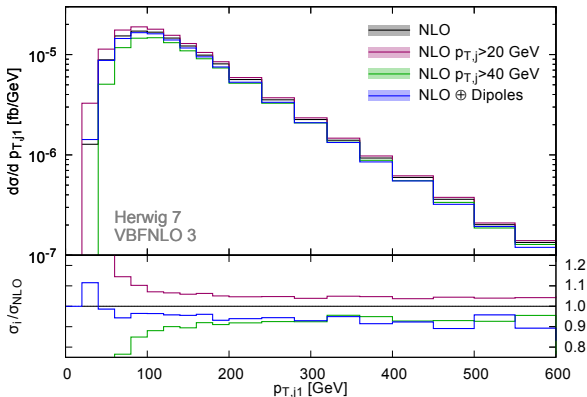
Vary transverse momentum cut of jets (default: $p_{T,j} > 30$ GeV)



- same effect when slightly raising $p_{T,j}$ cut
- additional parton splittings: if hard & wide-angle emission → [separate jet](#)
- → [reduces](#) energy and transverse momentum of [emitting parton](#)
- \leftrightarrow $p_{T,j}$ cut, VBF cut $m_{jj} > 600$ GeV

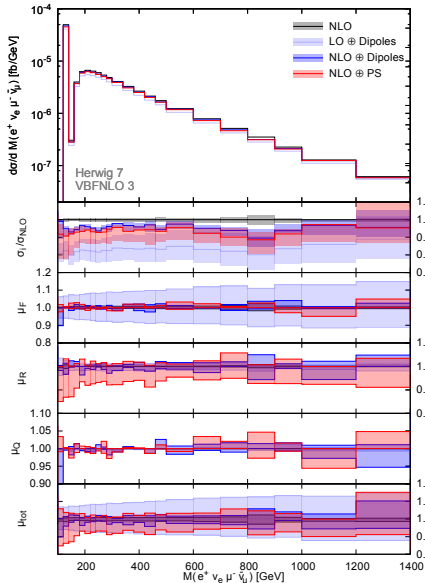
Migration Effects

Vary transverse momentum cut of jets (default: $p_{T,j} > 30$ GeV)



- less pronounced for small $p_{T,j1}$
 - VBF cut main source
- → migration of events across cut boundary
- ↔ generation-level vs. analysis-level cuts
- ⇒ no tuning of acceptance criteria required
- generation-level cuts nevertheless chosen weaker

Four-lepton Invariant Mass



← central scale $\mu_0 = p_{T,j1}$
transverse momentum of leading jet

← band: scale variation
 $\{\mu_F, \mu_R, \mu_Q\} / \mu_0 \in [\frac{1}{2}; 2]$
 $\mu_i / \mu_j \in [\frac{1}{2}; 2]$

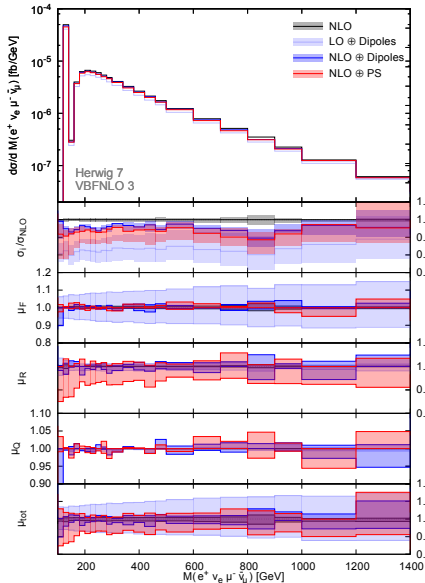
← factorization scale
 $\mu_F / \mu_0 \in [\frac{1}{2}; 2]$

← renormalization scale
 $\mu_R / \mu_0 \in [\frac{1}{2}; 2]$

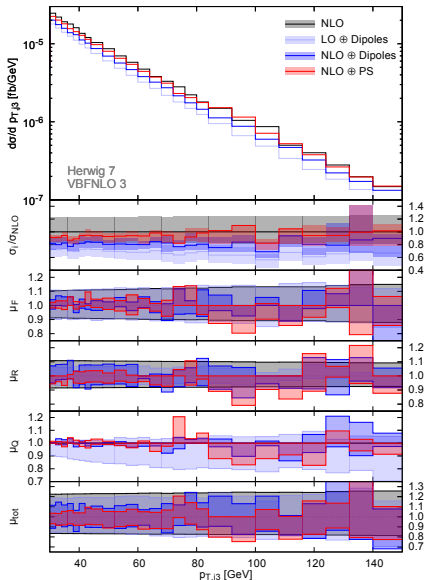
← shower scale
 $\mu_Q / \mu_0 \in [\frac{1}{2}; 2]$

← all three scales

Four-lepton Invariant Mass



- consistent variation of scales between hard process and parton shower
- large factorization scale dependence for LO result
- larger dependence for down variation of renormalization scale in angular-ordered shower:
larger $\alpha_S \rightarrow$ more splittings
 \rightarrow bigger migration effects
- small variations from shower-scale changes
- modest remaining overall uncertainty



- large scale variation bands for

- shower scale in LO ⊕ Dipoles
 - pure parton-shower effect

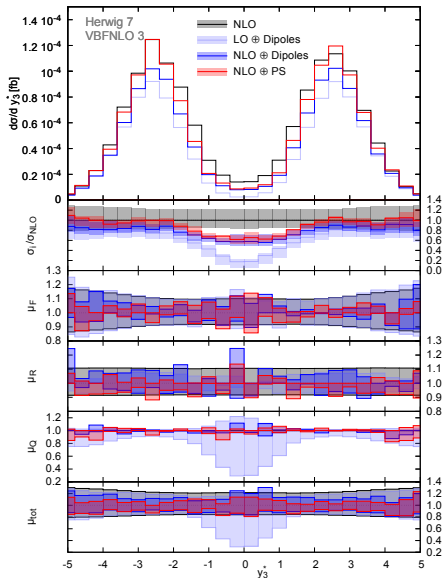
- fact./ren. scale in “NLO”
 - LO accuracy of observable

- reduced for both NLO + parton-shower curves

- still significant remaining uncertainty $\mathcal{O}(10 - 20\%)$

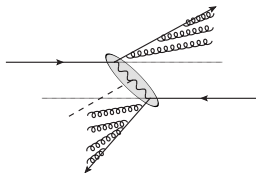
- → call for multi-jet merging

Rapidity of third jet



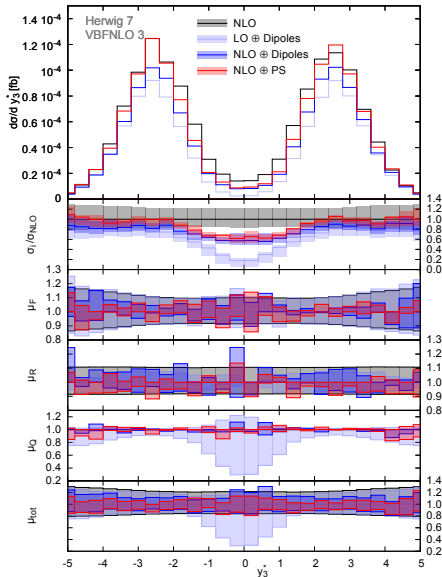
Rapidity of third jet
relative to two tagging jets

$$y_3^* = y_3 - \frac{y_1 + y_2}{2}$$



- VBF colour structure suppresses additional central jet radiation
- colour connection between tagging jet and remnant
- ↔ distinction from QCD-induced production

Rapidity of third jet

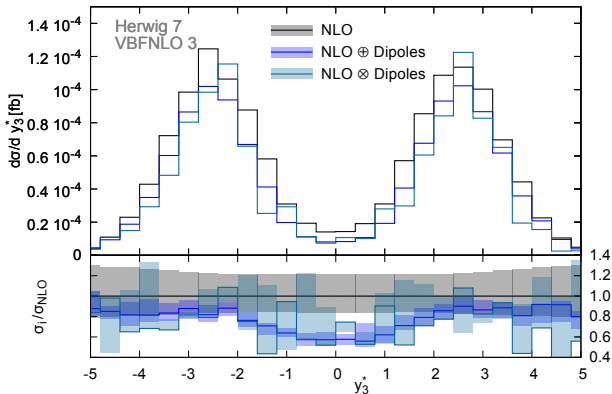


Rapidity of third jet
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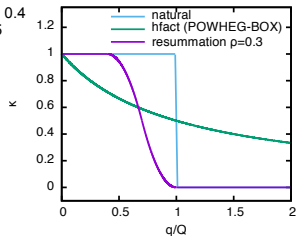
- impact of parton showers (+LO) long unclear
- Herwig predicts very low radiation in central region
- large shower-scale unc.
- stabilised when combining with NLO
- still reduction present
- scale variation bands not overlapping
- only small effects in forward region (mostly global normalization)

Rapidity of third jet – POWHEG

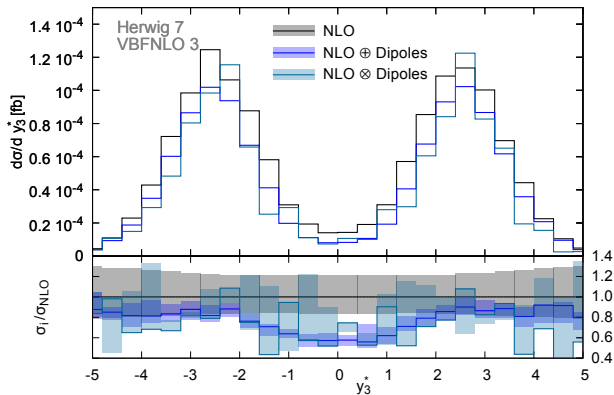


- POWHEG-like (\otimes) using resummation scheme [Plätzer]:

$$\kappa(Q, q; \rho) = \begin{cases} 1 & \text{for } q < (1 - 2\rho)Q \\ 1 - \frac{(1 - 2\rho - \frac{q}{Q})^2}{2\rho^2} & \text{for } (1 - 2\rho)Q < q < (1 - \rho)Q \\ \frac{(1 - \frac{q}{Q})^2}{2\rho^2} & \text{for } (1 - \rho)Q < q < Q \\ 0 & \text{for } q > Q \end{cases}$$



Rapidity of third jet – POWHEG

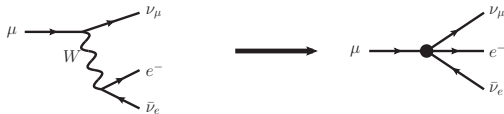


- band: joint variation $\mu_F = \mu_R = \mu_Q \in [\frac{1}{2}, 2] \mu_0$
- similar predictions from MC@NLO-like (\oplus) and POWHEG-like (\otimes) matching
- also holds for other distributions

Effective Field Theory

Assumption: new physics is heavy

Classic example: μ decay \rightarrow Fermi theory (t-channel W integrated out)



$$G_F = \frac{\sqrt{2}}{8} \frac{g^2}{m_W^2}$$

\Rightarrow Effective Lagrangian

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} + \sum_{d>4} \sum_i \frac{f_i^{(d)}}{\Lambda^{d-4}} \mathcal{O}_i^{(d)}$$

- operators \mathcal{O} contain SM fields only
- respect SM gauge symmetries
- suppressed by $1/\Lambda^{d-4}$ (Λ : scale of new physics)
 \rightarrow keep only leading order(s) (lowest dimension $d = 6$)
- building blocks:
 - Higgs field Φ
 - (covariant) derivative ∂^μ, D^μ
 - field strength tensors $G^{\mu\nu}, W^{\mu\nu}, B^{\mu\nu}$
 - fermion fields ψ

Unitarity Violation

Important gauge **cancellations** between different diagram types

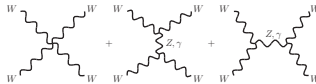
- longitudinal W scattering through quartic gauge boson vertex



high energy limit: centre-of-mass energy $\sqrt{s} \rightarrow \infty$

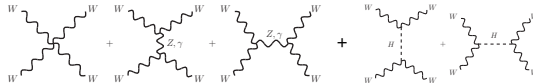
$$\mathcal{M}_{\text{quartic vertex}} \propto s^2 \rightarrow \text{cross section diverges} \quad \sigma \propto s^4/s = s^3 \rightarrow \infty$$

- add triple gauge boson vertices



$\mathcal{M}_{\text{quartic+triple vertices}} \propto s \rightarrow$ still **divergent**

- additional Higgs diagrams



remove divergence exactly $\sigma \propto 1/s \rightarrow 0$

Anomalous gauge couplings spoil cancellation \rightarrow stringent **tests**

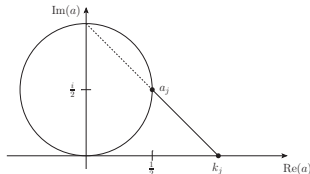
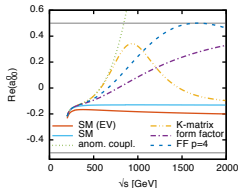
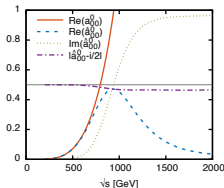
Anomalous gauge couplings spoil cancellation
 \leftrightarrow effects can become large \rightarrow **unitarity violation**

Several solutions:

- consider only unitarity-conserving phase-space regions
 throws away information \rightarrow reduced sensitivity
- (dipole) **form factor** multiplying amplitudes

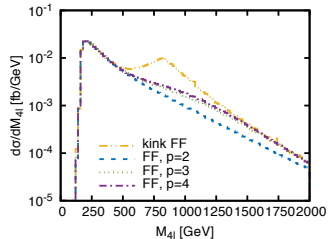
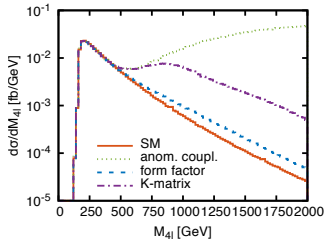
$$\mathcal{F}(s) = \frac{1}{\left(1 + \frac{s}{\Lambda_{\text{FF}}^2}\right)^n} \quad \Lambda_{\text{FF}}^2, n: \text{ free parameters}$$

- **K-matrix unitarization** [Alboteanu, Kilian, Reuter, Sekulla]
 based on partial-wave analysis [Jacob, Wick]
 project amplitude back onto **Argand circle**



Cross Section Results

Example Process: $pp (\rightarrow W^+ W^+ jj) \rightarrow e^+ \nu_e \mu^+ \nu_\mu jj$ at NLO QCD accuracy



- kink form factor (simplified projection for comparison):

$$F_{\text{kink}}(E) = \begin{cases} 1 & \text{for } E \leq \Lambda_{\text{FF,kink}} , \\ \left(\frac{\Lambda_{\text{FF,kink}}}{E}\right)^4 & \text{for } E > \Lambda_{\text{FF,kink}} , \end{cases}$$

- huge effects for un-unitarized result \leftrightarrow **unphysical**
- *K*-matrix method maximising contribution while staying in physical region
- \rightarrow study parton-shower and hadronization impact

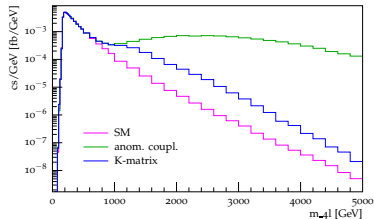
Combination with Parton Shower

Can also combine K-matrix in setup with parton shower

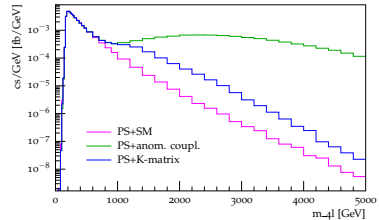
[VBFNLO 3 & Herwig 7]

Example: VBF- $W^+ W^+$ ($pp \rightarrow e^+ \nu_e \mu^+ \nu_\mu jj$)
anom. coupl.: $f_{S,1} = 100 \text{ TeV}^{-4}$

fixed-order NLO



NLO+PS (MC@NLO + dipole shower)



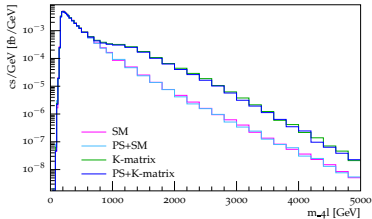
No significant shape changes in $m_{4\ell}$ when switching on PS
(integrated c.s. PS/NLO: -3.0% (SM) / -3.8% (K-matrix))

Can also combine K-matrix in setup with parton shower

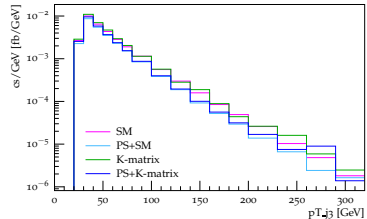
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Example: VBF- $W^+ W^+$ ($pp \rightarrow e^+ \nu_e \mu^+ \nu_\mu jj$)
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$m_{4\ell}$ – Comparison



$p_{j,3}^T$ – Comparison



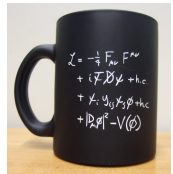
No significant shape changes in $m_{4\ell}$ when switching on PS
(integrated c.s. PS/NLO: -3.0% (SM) / -3.8% (K-matrix))

$\leftrightarrow p_{j,3}^T$ mostly sensitive to parton-shower effects

Parton-shower and scale variation effects in

$W^+ W^- jj$ production via vector-boson-fusion

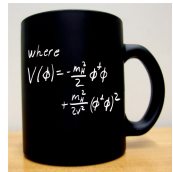
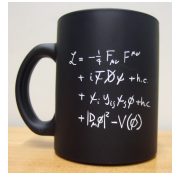
- important process for the LHC
 - Higgs properties – unitarity in WW scattering
 - testing anomalous (triple and) quartic gauge couplings
- study performed with **Herwig 7** & **VBFNLO 3**
- compatible behavior of both parton showers and matching schemes
- small parton-shower effects for distributions of variables already present at LO
 - mostly reduction of inclusive cross section due to additional jet radiation
- presence of central rapidity gap stabilised
- → multi-jet merging to further reduce uncertainties
- → study hadronization impact



Parton-shower and scale variation effects in

$W^+ W^- jj$ production via vector-boson-fusion

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Defined standardized interface between Monte Carlo tools and one-loop programs

→ [Binoth Les Houches Accord \(BLHA\)](#)

[[arXiv:1001.1307](#), [arXiv:1308.3462](#)]

- tree-level evaluation of matrix elements well under control
- modular structure of NLO calculations
- algorithms for treatment of infrared singularities (Catani-Seymour, FKS, ...)
- → incorporate one-loop matrix element information into MC tools

Distribution of tasks:

- MC tool:
 - cuts, histograms, parameters
 - Monte Carlo integration
 - phase space (→ [VBFNLO](#))
 - IR subtraction
 - Born, colour- and spin-correlated Born (only [BLHA1](#))
- One-loop provider (OLP):
 - one-loop matrix elements $2\Re(\mathcal{M}_{\text{LO}}^\dagger \mathcal{M}_{\text{virt}})$ (coefficients of ϵ^{-2} , ϵ^{-1} , ϵ^0 ; $|\mathcal{M}_{\text{LO}}|^2$)
 - Born, colour- and spin-correlated Born (only [BLHA2](#))

Setup stage via “contract” file

(needed for tools which generate code on the fly)

Run-time stage via binary interface (function calls) → fast

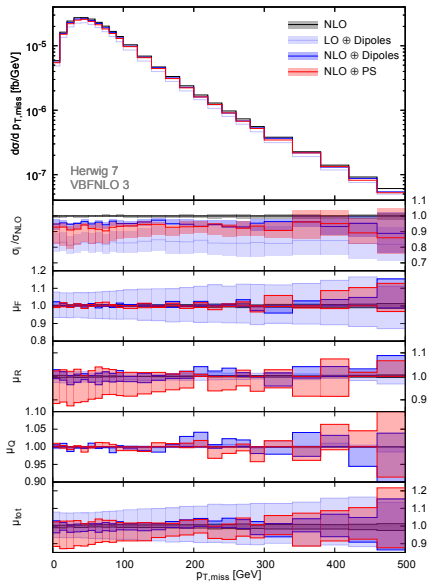
Generation-level cuts:

$$\begin{array}{ll} p_{T,j} > 20 \text{ GeV}, & |y_j| < 5.0, \\ \text{anti-}k_T \text{ jets with } R = 0.4, & \text{b-quark veto} \\ p_{T,\ell} > 15 \text{ GeV}, & |y_\ell| < 3.0, \\ m_{e^+, \mu^-} > 15 \text{ GeV}, & \\ m_{j_1, j_2} > 400 \text{ GeV}, & |y_{j_1} - y_{j_2}| > 3.0 \end{array}$$

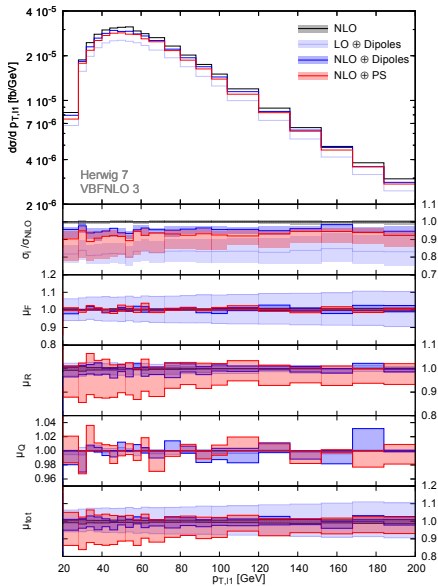
Analysis-level cuts:

$$\begin{array}{ll} p_{T,j} > 30 \text{ GeV}, & |y_j| < 4.5, \\ \text{anti-}k_T \text{ jets with } R = 0.4, & \text{b-quark veto} \\ p_{T,\ell} > 20 \text{ GeV}, & |y_\ell| < 2.5, \\ m_{e^+, \mu^-} > 15 \text{ GeV}, & \\ m_{j_1, j_2} > 600 \text{ GeV}, & |y_{j_1} - y_{j_2}| > 3.6 \end{array}$$

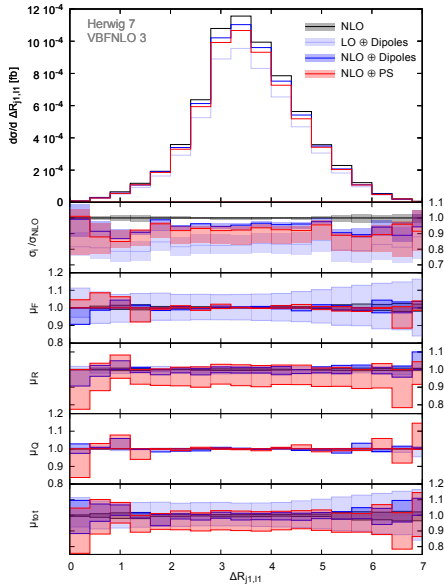
Missing Transverse Momentum



Transverse Momentum of Leading Lepton



R Separation of Leading Jet and Leading Lepton



$$\Delta R = \sqrt{\Delta y^2 + \Delta \phi^2}$$

Jacobian peak at $\Delta R_{j1,l1} = \pi$

[Cacciari, Dreyer, Karlberg, Salam, Zanderighi]

- NNLO effects well approximated by NLO plus parton-shower results

